

# Origins of the Lee Lecture and Reflections on Professor Lee

Jonathan P. Stewart, PhD, PE, NAE

*UCLA Samueli Engineering*



ASCE Geo-Institute Los Angeles  
Queen Mary  
May 7, 2026

# Establishment of the Lee Lecture...

## Motivation:

- Enhance prestige of Spring Seminar
- Honor a pioneer in our field & raise awareness of his contributions to Geotechnical Engineering
- Similar lectures: Casagrande Lecture (Boston), Martin Kapp Lecture (NYC), Buchanan Lecture (Texas A&M)

# Establishment of the Lee Lecture...

## Motivation

### Vision:

- “The Kenneth L. Lee Lecture will be presented annually at the Geotechnical Group’s Spring Seminar by a noted geotechnical professional who has made significant contributions either to Geotechnical Engineering practice in southern California or to research associated with the design of earth structures or Geotechnical Earthquake Engineering”

# Establishment of the Lee Lecture...

Motivation

Vision

Organizing committee (~ 2002 – May 2004):

- Anthony Augello, Golder
- Ed Kavazanjian, USC / Geosyntec
- Jasmina Matasovic
- Allen Yourman, Diaz-Yourman Associates
- Jon Stewart, UCLA

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Vision

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Inaugural event May 5, 2004:

- Co-awardees: J. Michael Duncan, I.M. Idriss



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**Inaugural event May 5, 2004:**

- Co-awardees: J. Michael Duncan, I.M. Idriss
- Attended by Lee family members



# Establishment of the Lee Lecture...

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**Inaugural event May 5, 2004:**

- Co-awardees: J. Michael Duncan, I.M. Idriss
- Attended by Lee family members
- ... and former students



*Allen Yourman*

John Lee  
(brother)





Four Lee children



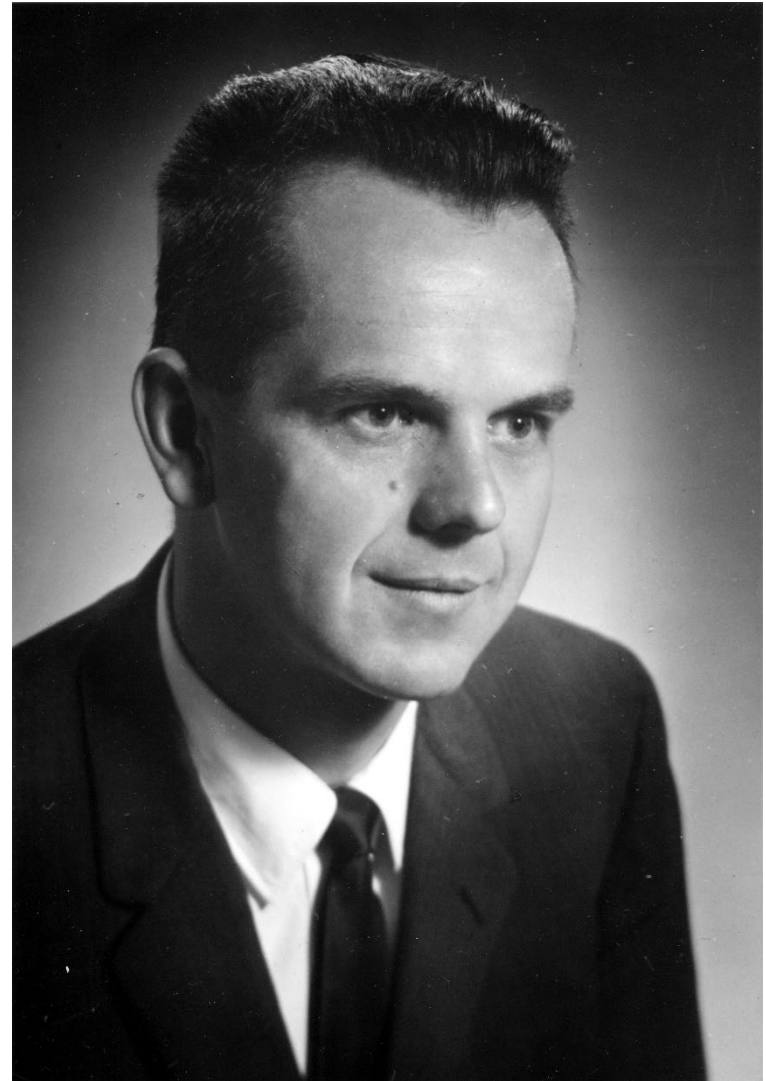




# Kenneth L. Lee

## Biographical information:

- Born 1931, Albert Canada
- BS (1955), MS (1958) U. Alberta
- Soil Engineer in Canada, 1958-1961
- PhD UCB (1965), Advisor HB Seed
- UCLA faculty, 1964-1978
- Died in skiing accident, 3/1978



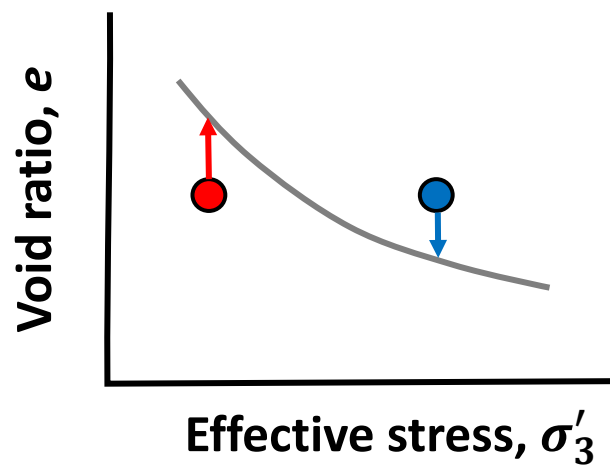
# Kenneth L. Lee

Biographical information

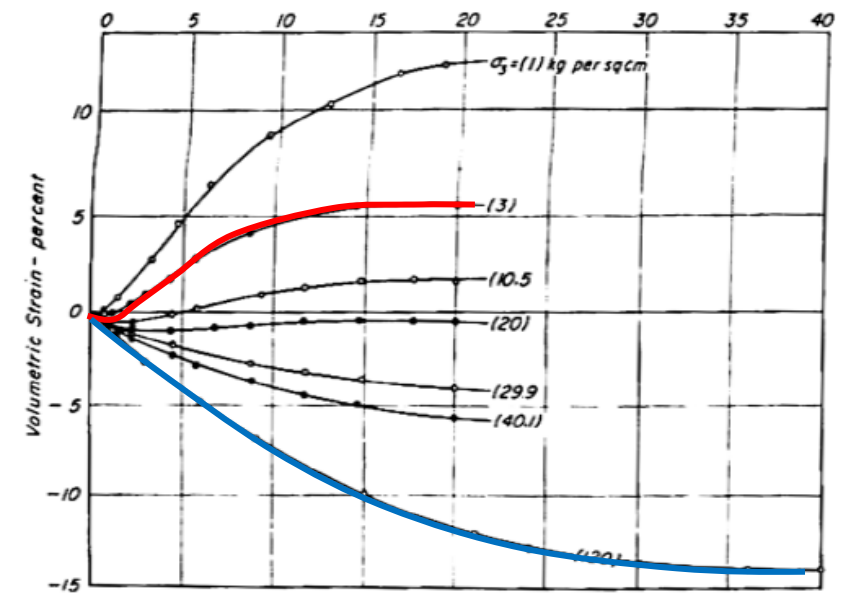
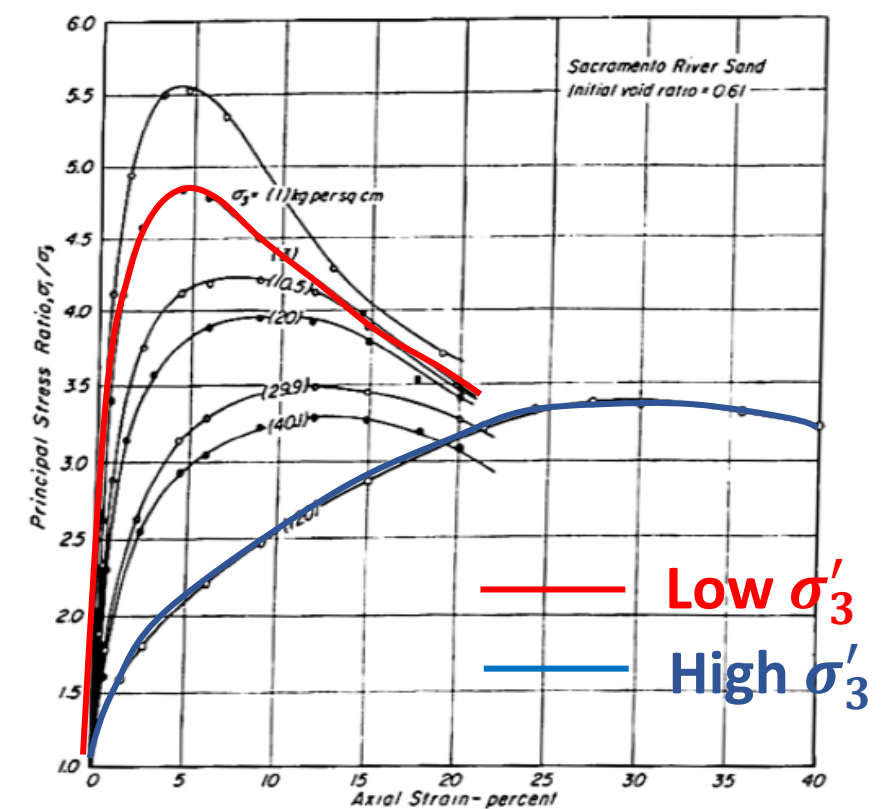
Technical contributions

- Dilatancy effects on drained behavior of sands

## Dense sands



Lee and Seed, 1967



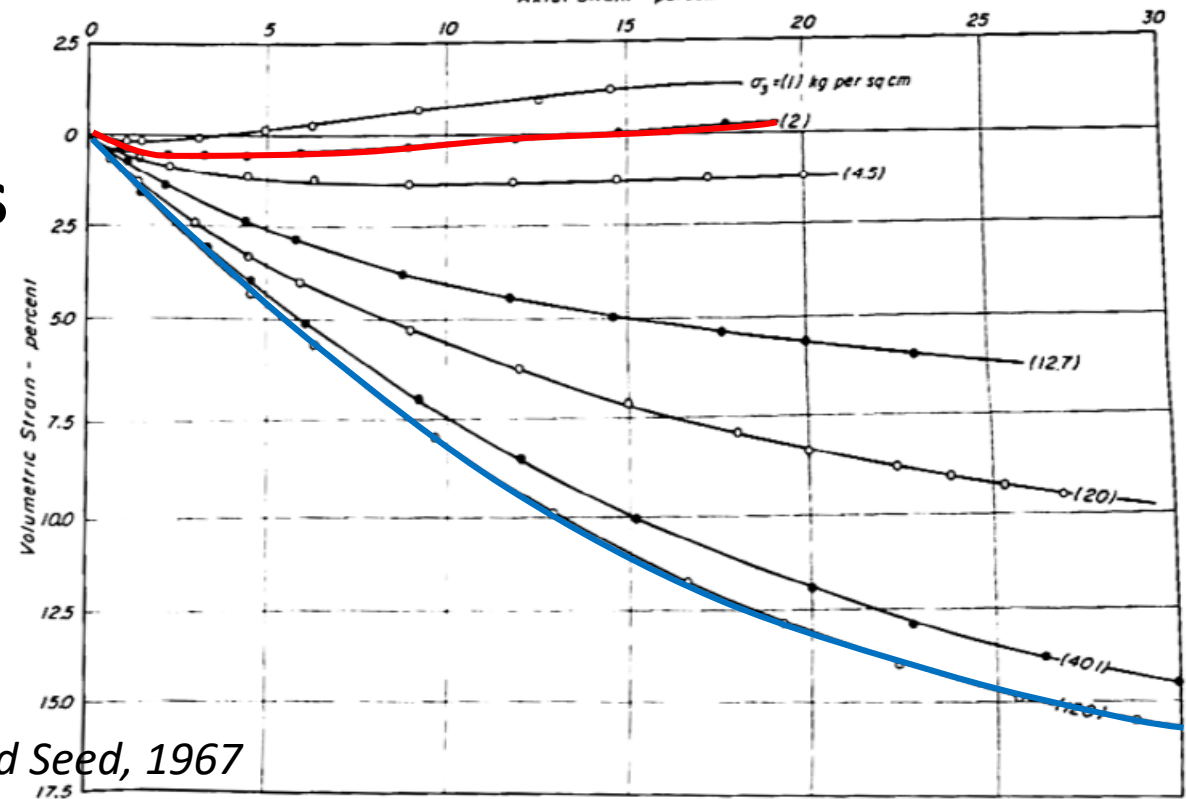
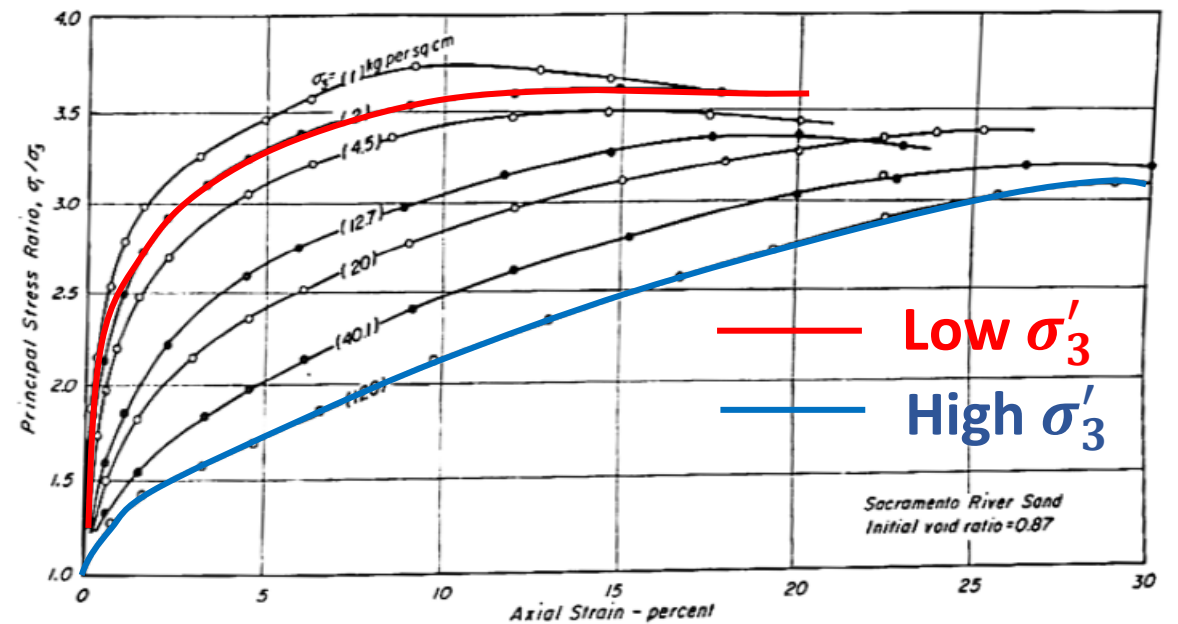
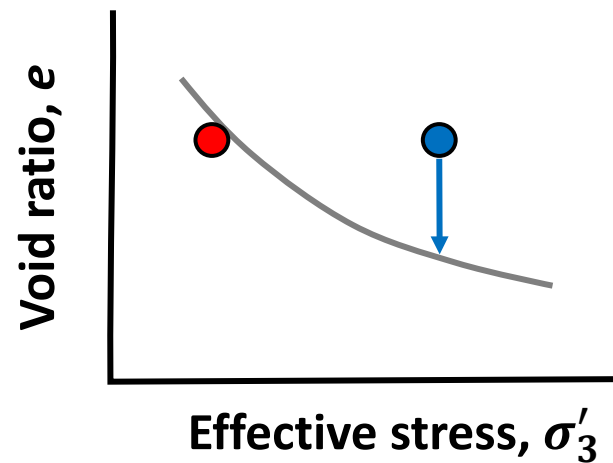
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Biographical information

Technical contributions

- Dilatancy effects on drained behavior of sands

## Loose sands



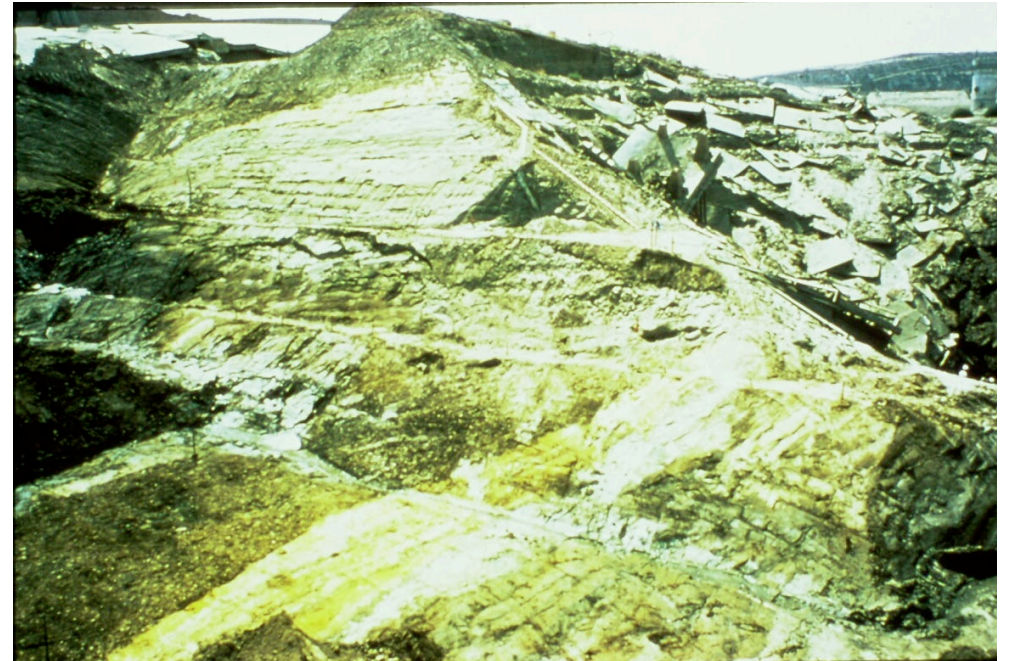
Lee and Seed, 1967

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Biographical information

Technical contributions

- Dilatancy effects on drained behavior of sands
- Investigation of Lower San Fernando Dam (1971-1973); co-lead with Seed of blue ribbon investigation panel

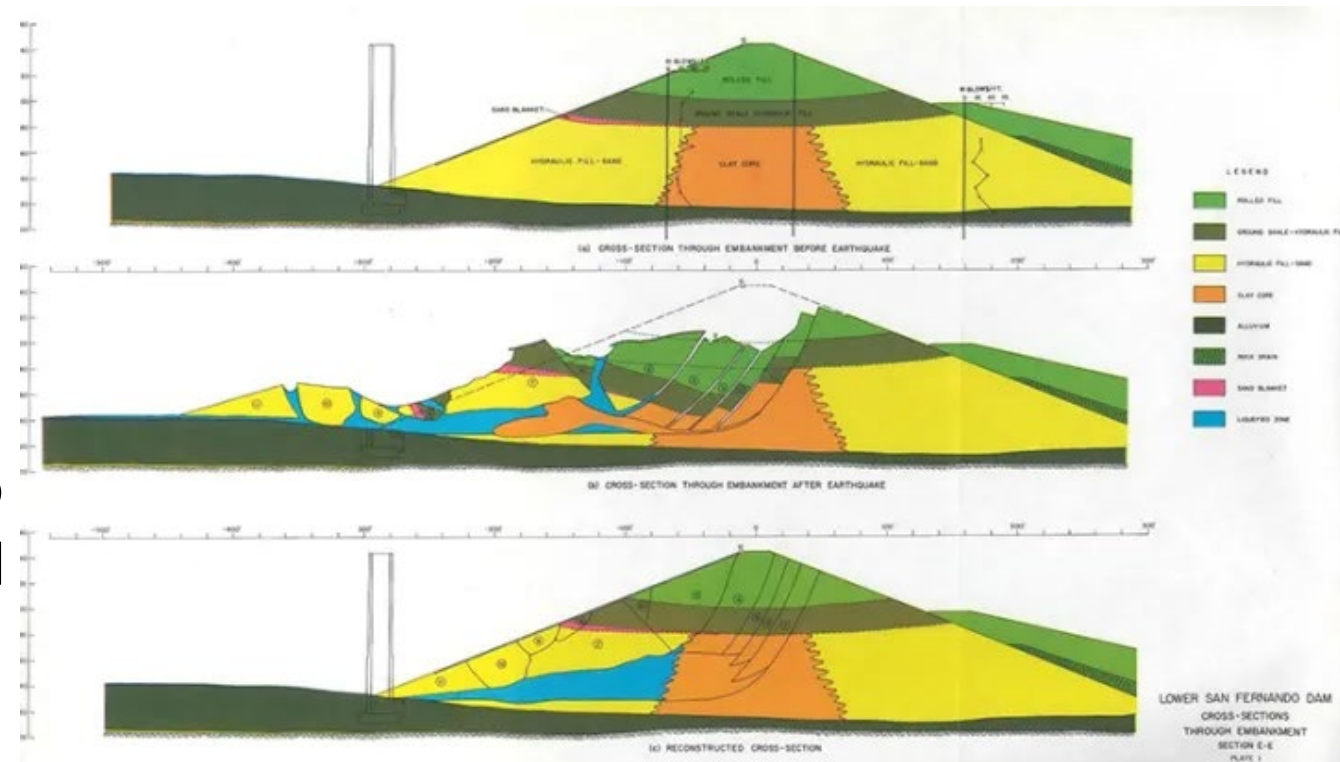


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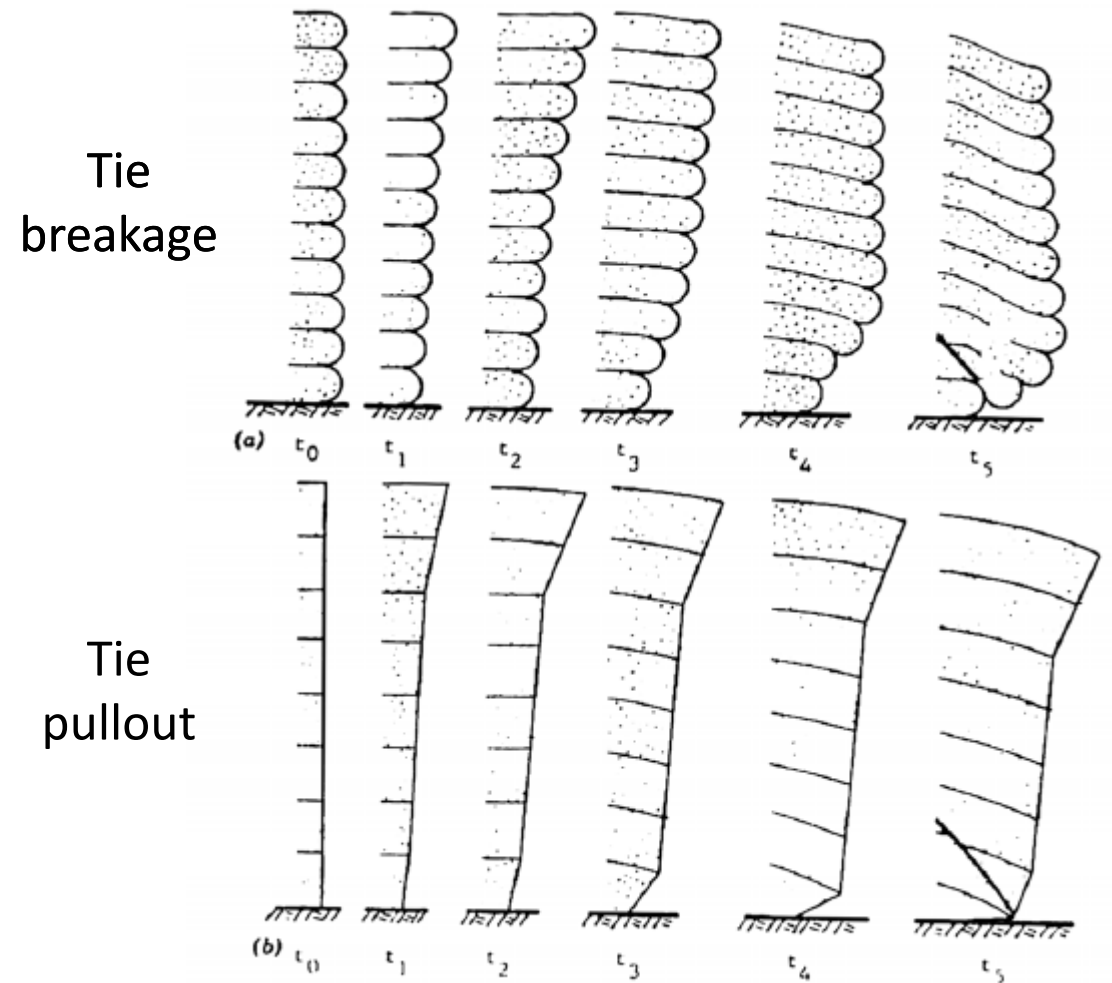
*Seed et al., 1973*

# Kenneth L. Lee

Biographical information

Technical contributions

- Dilatancy effects on drained behavior of sands
- Investigation of Lower San Fernando Dam (1971-1973); co-lead with Seed of blue ribbon investigation panel
- Seismic design of reinforced soil walls



*Richardson and Lee, 1975*

# Kenneth L. Lee

Biographical information

Technical contributions

## Major awards

- Norman Medal (1968, 1977)
- Huber Prize (1970)
- Collingwood Prize (1970)
- Middlebrooks Award (1971)
- James R. Croes Medal (1978)

# Kenneth L. Lee

Biographical information

Technical contributions

Major awards

Notable students

Ron Chaney, PhD, Humboldt State University

Claud Corvino, Nichols Consulting

Dan Feger, Burbank Airport Authority

Jean Hill, PhD, URS

Boris Korin, RT Frankian and Associates

Marshall Lew, PhD, Leroy Crandall and Associates

Bart Patton, Kleinfelder

Greg Richardson, PhD, Richardson and Associates

Wolfgang Roth, Postdoc, URS

Jean Marie Vagernon, PhD, France

Fernando Valenzuela, PhD Candidate, Chile

James Weaver, Geomatrix

Bill Wolfe, PhD, Ohio State University

Allen Yourman, Diaz-Yourman and Associates

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**Allen Yourman, Diaz-Yourman and Associates**

# Kenneth L. Lee

Biographical information

Technical contributions

Major awards

Notable students

Quotes compiled by J.M. Duncan  
(2004)

*I continued on at UCLA with the intent to get an MS in structural engineering. One day Ken came up to me in the hallway and asked if I had considered going into geotechnical engineering. I decided that he was just so enthusiastic that he thought almost everybody should be a geotechnical engineer.*

- Steve Haley

# Kenneth L. Lee

Biographical information

Technical contributions

Major awards

Notable students

Quotes compiled by J.M. Duncan  
(2004)

*Other faculty members told me that they could always hear when Ken was in the classroom next door, because they could hear the students laughing at his jokes and stories.*

- Poul Lade

# Kenneth L. Lee

Biographical information

Technical contributions

Major awards

Notable students

Quotes compiled by J.M. Duncan  
(2004)

*He wrote papers that you could understand.....He taught me how to write.*

- Ron Chaney

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Biographical information

Technical contributions

Major awards

Notable students

Quotes compiled by J.M. Duncan  
(2004)

*I can truthfully say that I never heard  
him speak ill of anyone.*

- Jim Mitchell

# Kenneth L. Lee

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Notable students

Quotes compiled by J.M. Duncan  
(2004)

*The world is a better place for Ken having been here. He contributed enormously to our welfare and he will be missed by all.*

- H Bolton Seed

# Kenneth L. Lee

Biographical information

Technical contributions

Major awards

Notable students

Quotes compiled by J.M. Duncan  
(2004)

*The best possible use of life is to spend  
it for something that outlasts it.*

- Ken Lee



# 20<sup>th</sup> Kenneth L. Lee Lecture

## Integration of Non-Ergodic Site Response into NEHRP Provisions & ASCE-7

Jonathan P. Stewart, PhD, PE, NAE

*UCLA Samueli Engineering (& PUC Member)*



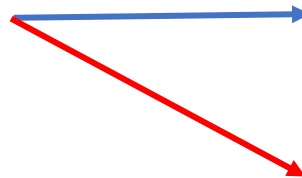
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Queen Mary  
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# Site Response in the NEHRP Provisions

- Chapter 21: Site-specific ground motion procedures



21.2: PSHA for specific location  
with user-selected source and  
ground motion models (GMMs)



Use “ergodic” site response  
model (site term in GMM)

Use site-specific site  
response model

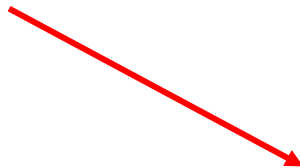
*Section 21.1*

# Site Response in the NEHRP Provisions

- Chapter 21: Site-specific ground motion procedures



Reference-site ground motion  
from USGS NSHM



Use site-specific site  
response model

*Section 21.1*

# IT3 / Sub-Issue Team 5

CB Crouse, AECOM, former PUC member

Gyimah Kasali, Rutherford and Chekeyne,  
PUC member

Debra Murphy, Slate, PUC member

Andrew Makdisi, USGS, PUC liaison

Silvia Mazzoni, consultant, IT3 and ASCE7

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# Outline

Current procedures

Issues motivating new procedures

Site-specific site response approach

Hybrid ground motions approach

Other technical improvements

Organization and status of document

# Outline

Current procedures

Issues motivating new procedures

**Site-specific site response approach**

**Hybrid ground motions approach**

Other technical improvements

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*Alternative approaches  
in 21.1*

# Outline

## **Current procedures**

Issues motivating new procedures

Site-specific site response approach

Hybrid ground motions approach

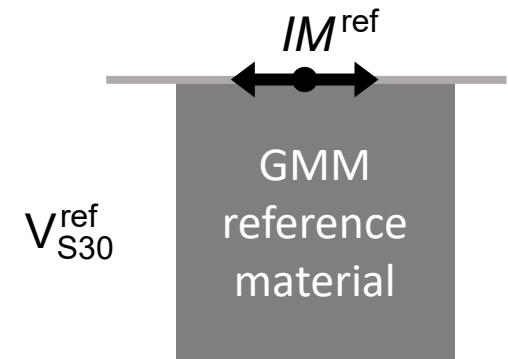
Other technical improvements

Organization and status of document

# Current procedures

## Base motion (21.1.1)

- Ground motion model reference motion

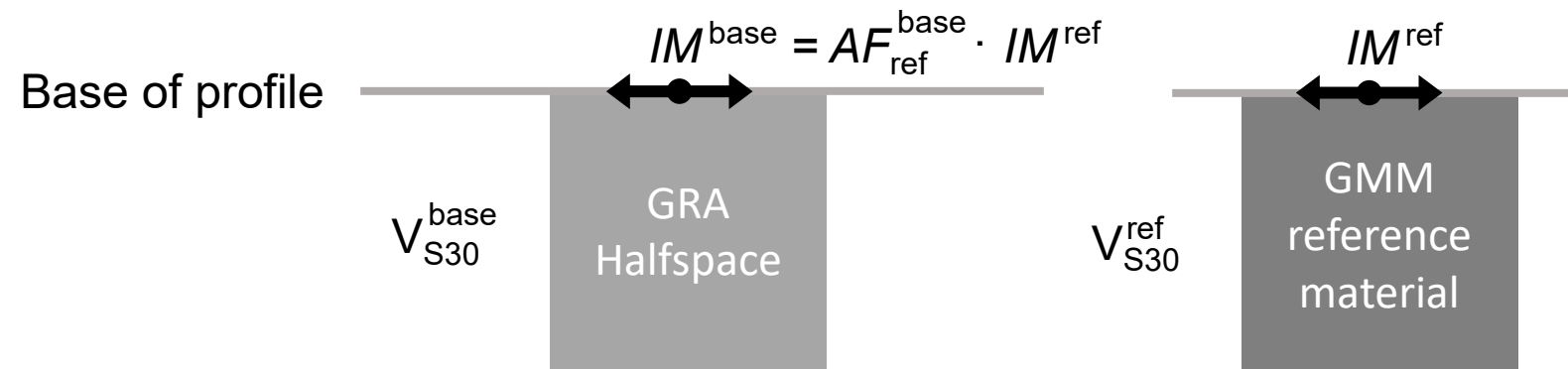


*Kramer & Stewart 2025*

# Current procedures

## Base motion (21.1.1)

- Ground motion model reference motion
- Base of profile



Five time series selected for compatibility with  $IM^{base}$

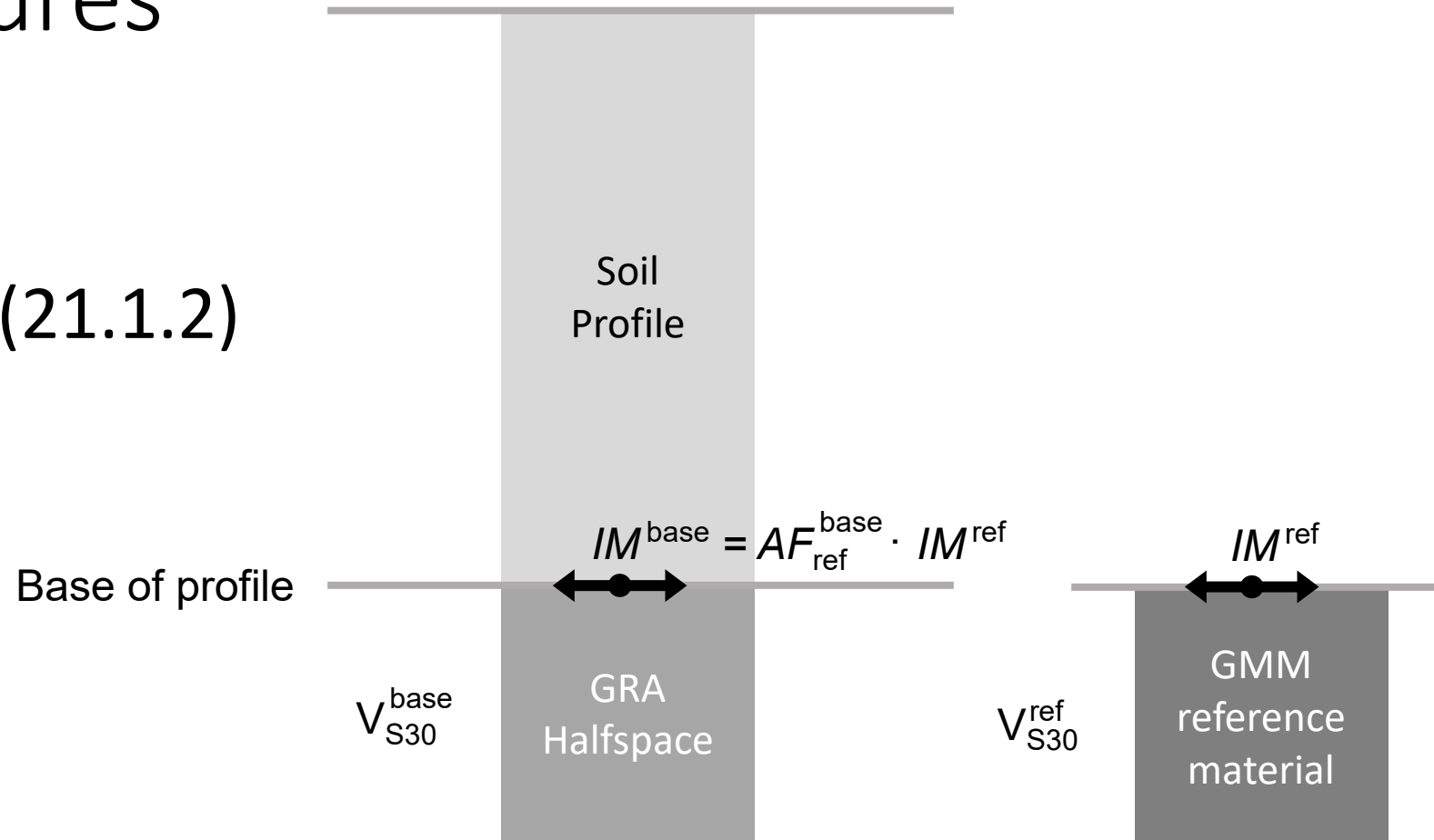
*Kramer & Stewart 2025*

# Current procedures

Base motion (21.1.1)

Site condition model (21.1.2)

- $V_S$  profile
- Nonlinear properties



*Kramer & Stewart 2025*



# Outline

Current procedures

**Issues motivating new procedures**

Site-specific site response approach

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# Issues motivating new procedures

Period limitation of ground response analysis (GRA)

Hazard (risk) level not preserved

Lack of guidance on non-ergodic site response



***More to come***

# Issues motivating new procedures

Period limitation of GRA

Hazard (risk) level not preserved

Lack of guidance on non-ergodic site response

Content dated with respect to

- Site characterization

} ***V<sub>S</sub>, nonlinearity***

# Issues motivating new procedures

Period limitation of GRA

Hazard (risk) level not preserved

Lack of guidance on non-ergodic site response

Content dated with respect to

- Site characterization
- Analysis procedures



***Liquefiable soils***

***Long periods***

***Current methods require input motion time series (thus precluding RVT)***

# Outline

Current procedures

Issues motivating new procedures

**Site-specific site response approach**

Hybrid ground motions approach

Other technical improvements

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# Site-specific approach

Functional definitions

Model elements

Implementation in hazard  
calculations

Example results

Allowable reductions

# Site-specific approach: *Functional definitions*

## Ergodic site response:

- Models developed from diverse (global) data set
- Conditioned on site parameters (e.g.,  $V_{S30}$  and others)
- Used in National Seismic Hazard Model (NSHM)
- Preserves hazard levels, but application to specific site is accompanied by large uncertainty

*Applies to  
Section 21.2*

# Site-specific approach: *Functional definitions*

Ergodic site response:

Site-specific, non-ergodic site response:

- Applicable to specific site, no site-to-site variability ( $\phi_{S2S}=0$ )
- Model uncertainty treated as epistemic
- Merged with reference rock spectrum in relatively rigorous manner that preserves hazard level

# Site-specific approach

Functional definitions

## **Model elements:**

- **Mean model**
- **Aleatory variability**
- **Epistemic uncertainty**

Implementation in hazard calculations

Example results

Allowable reductions

## *Mean Site Response Model*

$$\mu_{\ln Z} = \underbrace{F_E + F_P}_{\text{Ergodic source \& path}} + \mu_{\ln AF}$$

Ergodic source & path

$\mu_{\ln AF}$ : mean site amplification

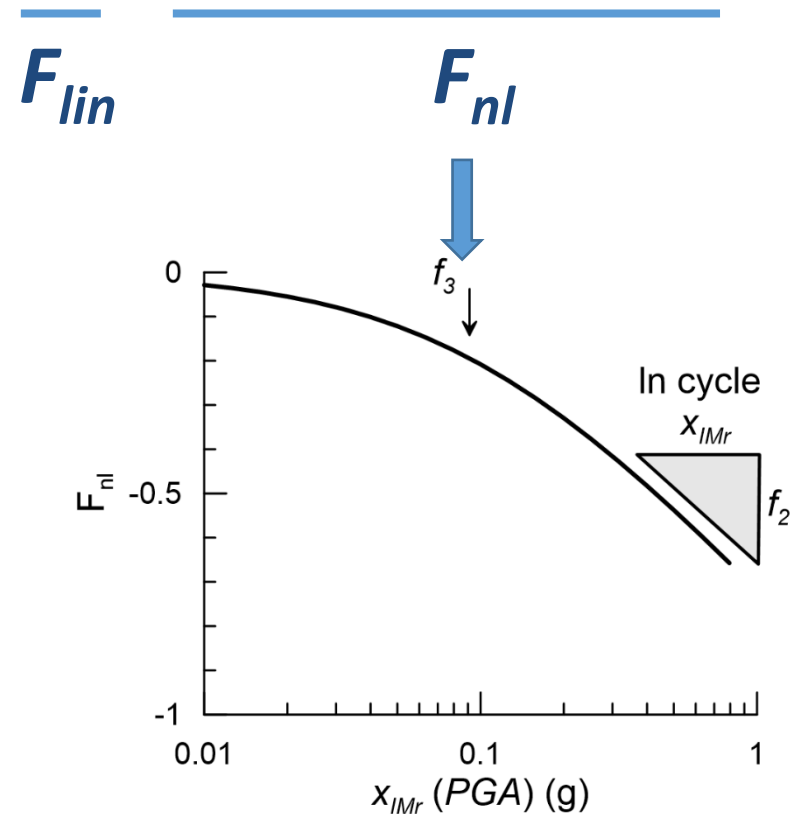
# Mean Site Response Model

## Function

Can be derived from:

- Approach 1: Ground motion data
- Approach 2: Ground response analyses
- Combinations of 1 & 2

$$\mu_{\ln AF} = f_1 + f_2 \ln \left( \frac{x_{IMr} + f_3}{f_3} \right)$$



## *Aleatory Variability*

GMM equation

$$\mu_{\ln Z} = F_E + F_P + \mu_{\ln AF}$$

# *Aleatory Variability*

GMM equation

$$\underbrace{\mu_{\ln Z}} = \underbrace{F_E} + \underbrace{F_P + \mu_{\ln AF}}$$

Residual terms

$$\delta_{ij} \quad \eta_{Ei} \quad \delta W_{ij}$$

# *Aleatory Variability*

GMM equation

$$\underbrace{\mu_{\ln Z}} = \underbrace{F_E} + \underbrace{F_P + \mu_{\ln AF}}$$

Residual terms

$$\delta_{ij} \quad \eta_{Ei} \quad \delta W_{ij}$$



Std. deviation terms

$$\sigma_{\ln}$$

$$\tau_{\ln}$$

$$\phi_{\ln}$$

# Aleatory Variability

GMM equation

$$\underbrace{\mu_{\ln Z}} = \underbrace{F_E} + \underbrace{F_P + \mu_{\ln AF}}$$

Residual terms

$$\delta_{ij} \quad \eta_{Ei} \quad \delta W_{ij}$$



Std. deviation terms

$$\sigma_{\ln}$$

$$\tau_{\ln}$$

$$\phi_{\ln}$$



**Null for site-specific,  
non-ergodic site  
response**

~~Site to site variability,  $\phi_{S2S}$~~

Single-station variability,  $\phi_{SS}$

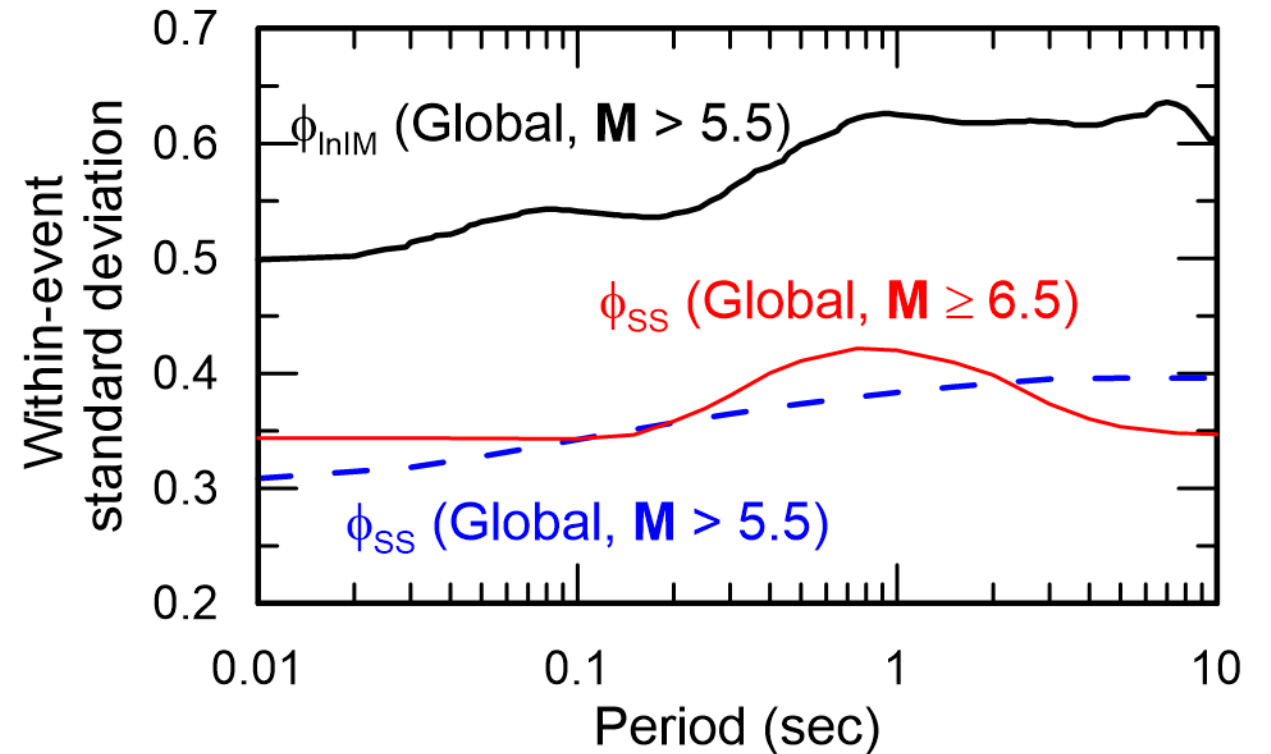
$$\sigma_{\ln} = \sqrt{\tau_{\ln}^2 + \phi_{SS}^2}$$

# *Aleatory Variability*

GMM equation

Residual terms

Std. deviation terms



*Kramer and Stewart, 2025*

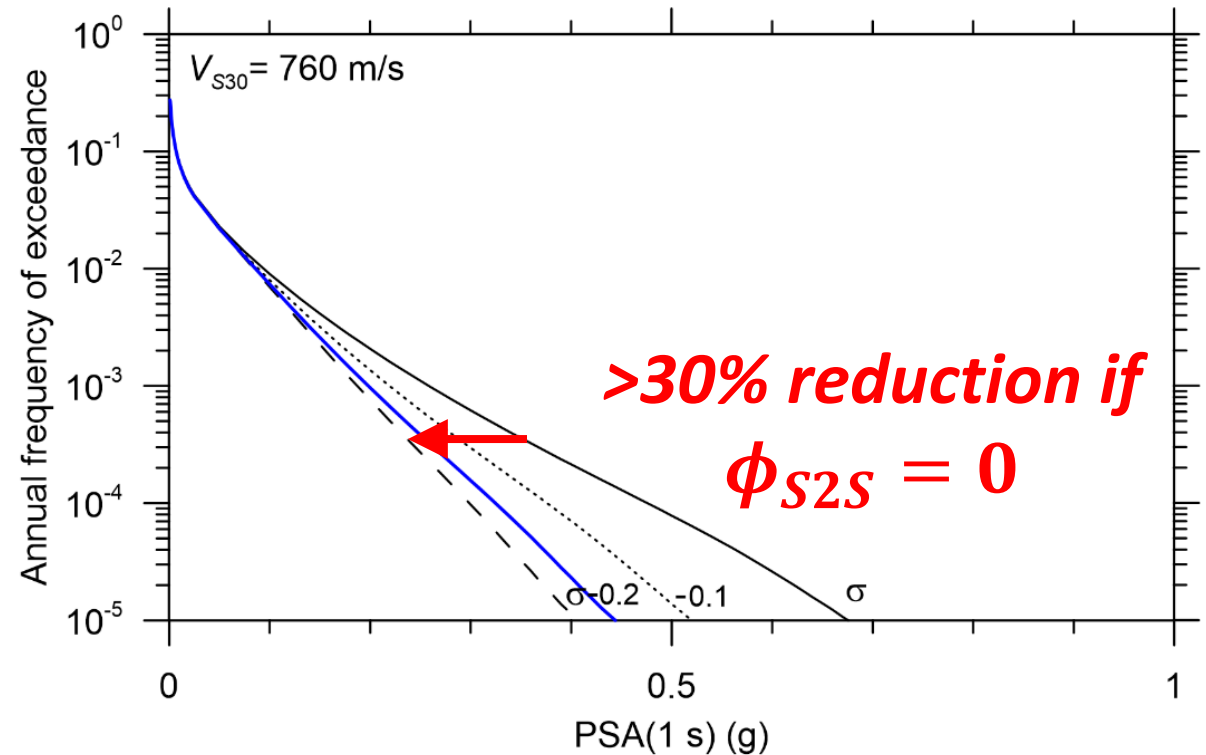
# Aleatory Variability

GMM equation

Residual terms

Std. deviation terms

Effect of non-ergodic site response on hazard



# Site-specific approach

Functional definitions

Model elements

**Implementation in hazard  
calculations**

Example results

Allowable reductions

# *Hazard Analysis Implementation*

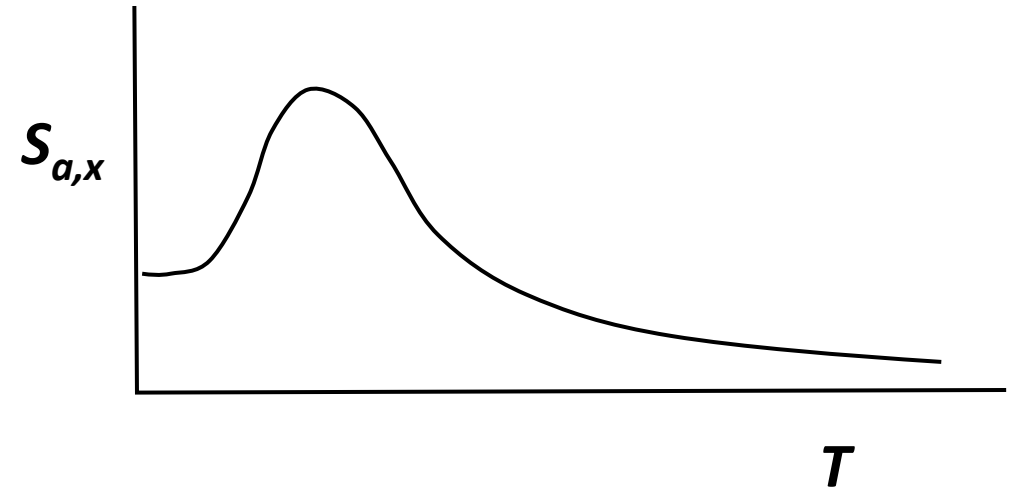
Hybrid: PSHA for reference site with deterministic site effect

PSHA with convolution

PSHA with modified GMM in hazard integral

# Hybrid

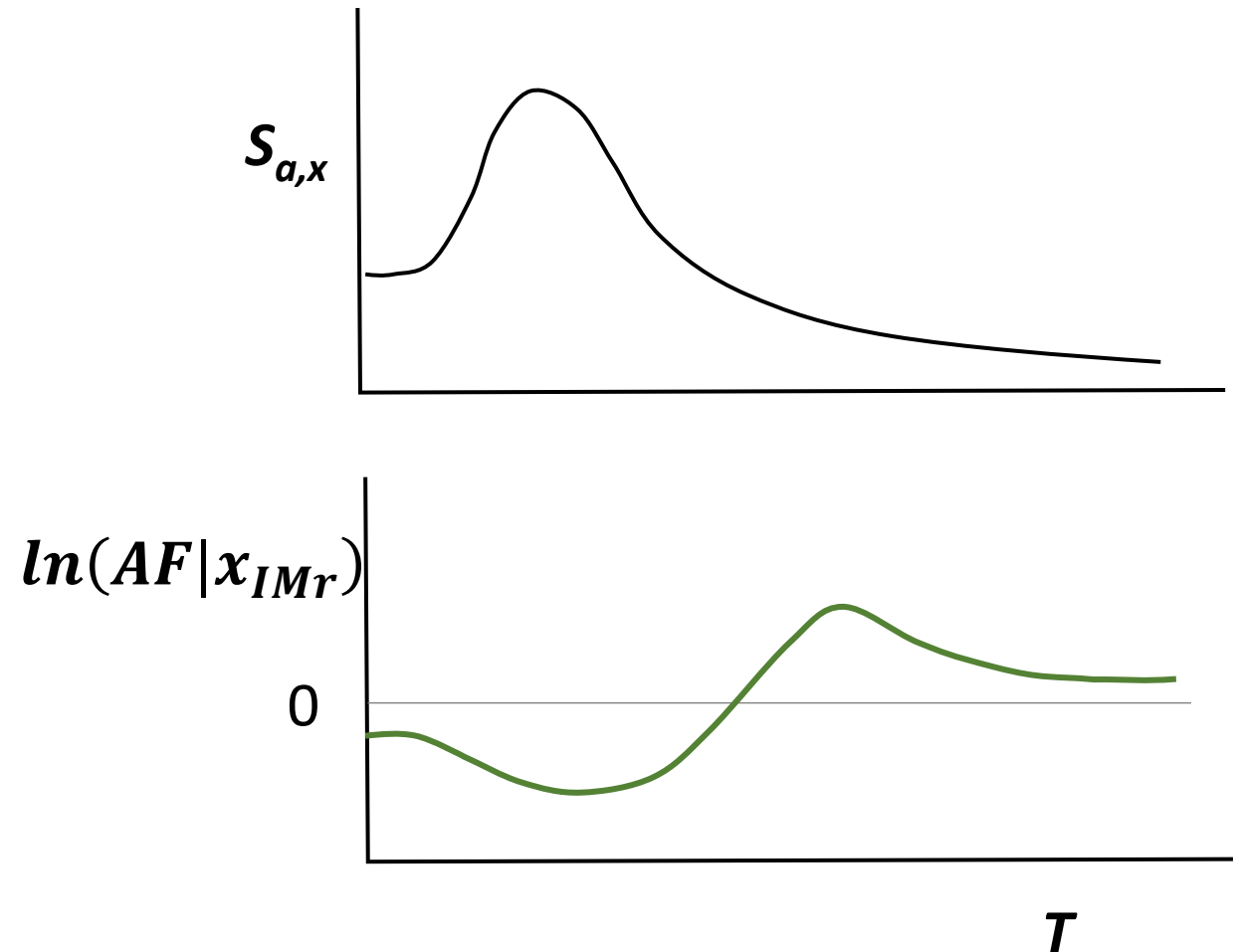
Develop reference site ( $X$ ) hazard curves & UHS ordinates



# Hybrid

Develop reference site ( $X$ ) hazard curves & UHS ordinates

Develop period-dependent amplification ( $AF$ ) corresponding to reference site ground motion



# Hybrid

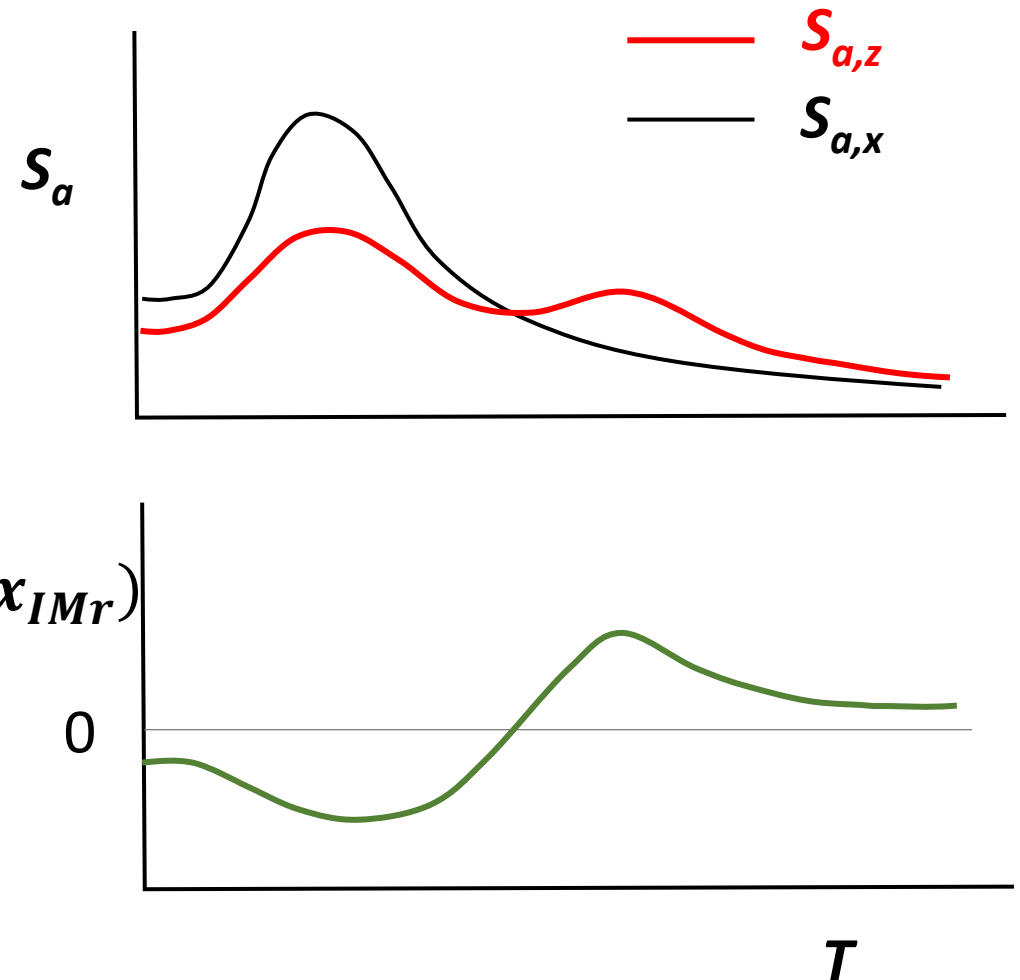
Develop reference site ( $X$ ) hazard curves & UHS ordinates

Develop period-dependent amplification ( $AF$ ) corresponding to reference site ground motion

Compute ground surface motion:

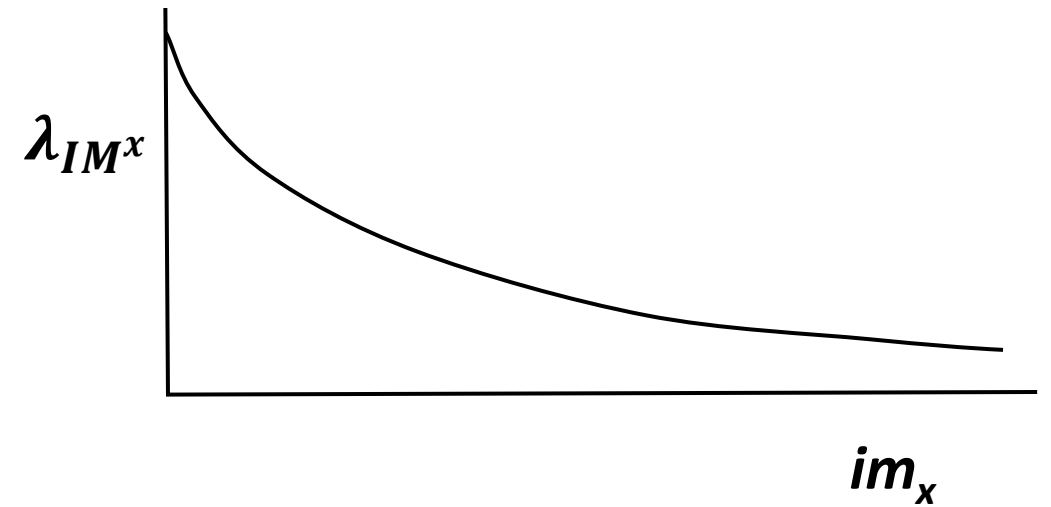
$$\ln(S_{a,z}) = \ln(S_{a,x}) + \ln(AF|x_{IMr})$$

NRC Approach 2 (see also Cramer 2003)



# Convolution

Develop reference site ( $X$ ) hazard curves & UHS ordinates



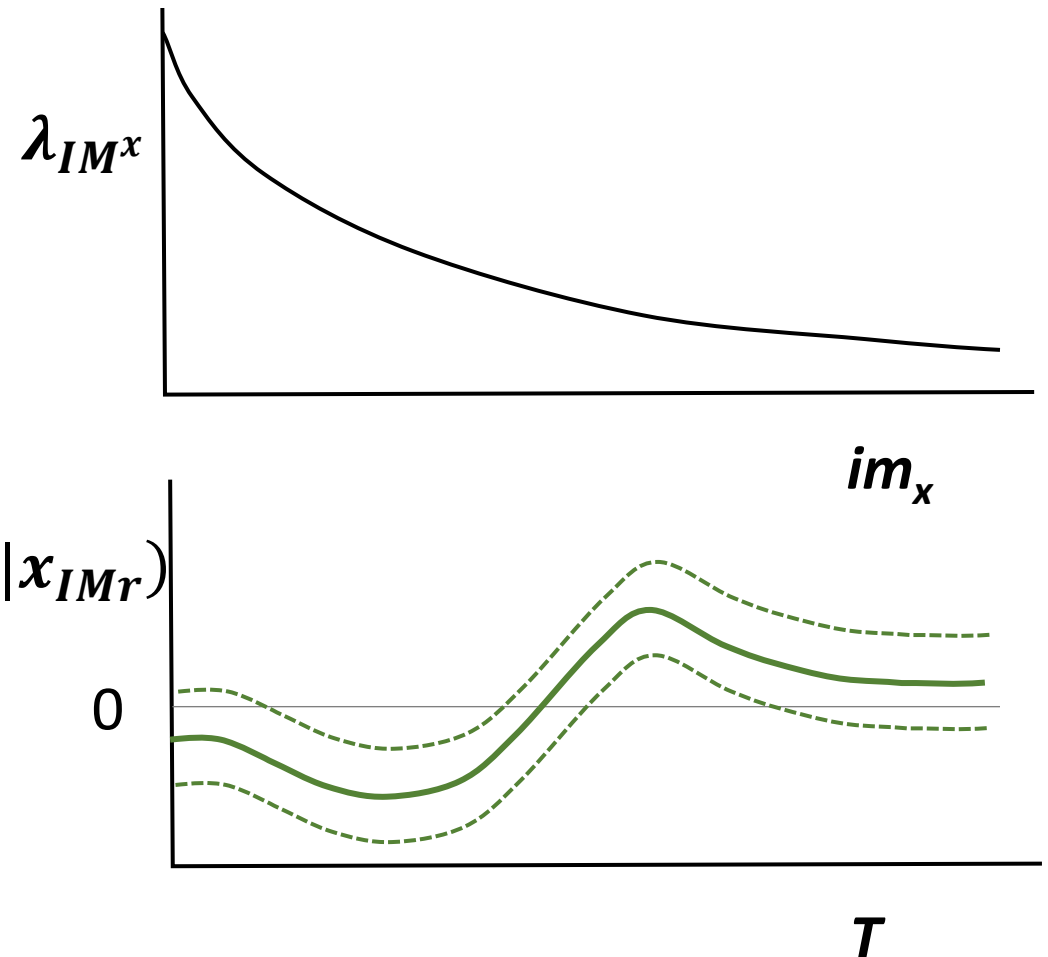
# Convolution

Develop reference site ( $X$ ) hazard curves & UHS ordinates

Develop  $x_{IMr}$ -dependent probabilistic amplification model:

$$\mu_{\ln AF} = f_1 + f_2 \left( \frac{x_{IMr} + f_3}{f_3} \right)$$

$$\phi_{\ln AF}$$



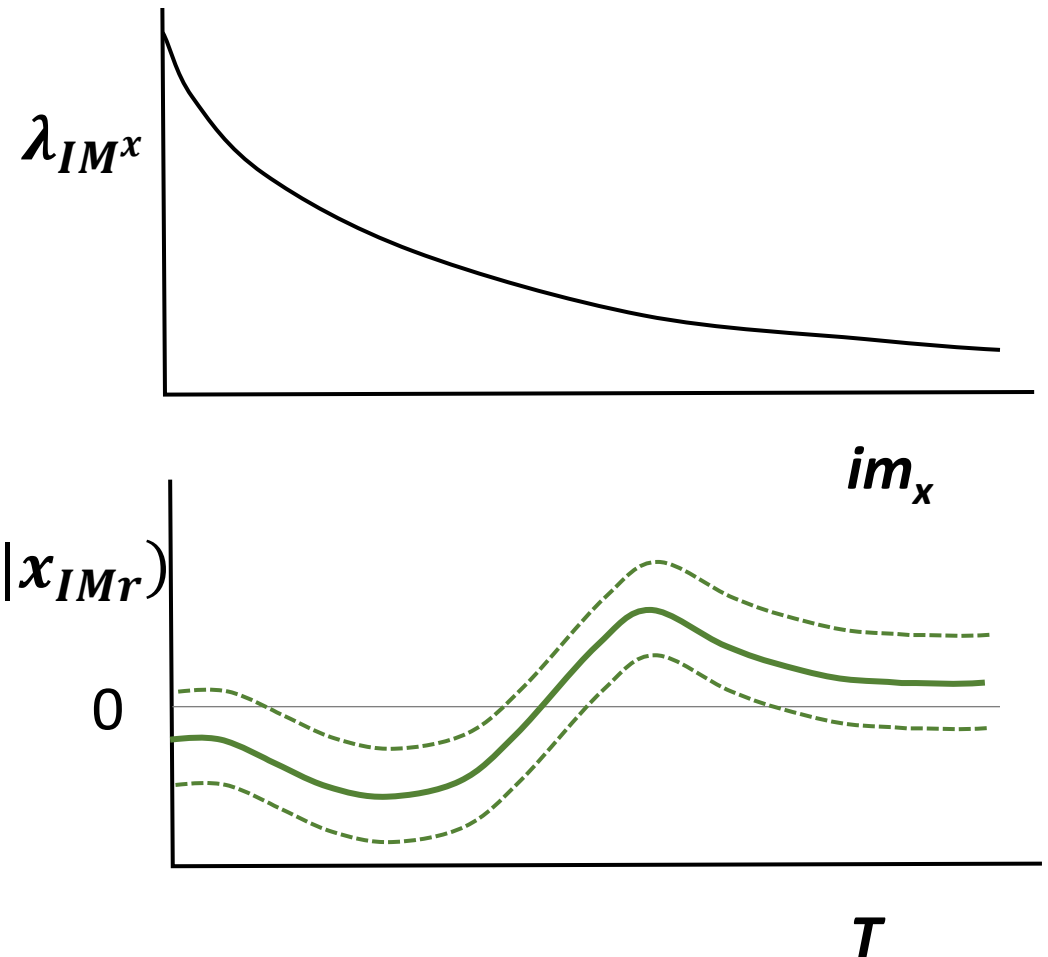
# Convolution

Develop reference site ( $X$ ) hazard curves & UHS ordinates

Develop  $x_{IMr}$ -dependent probabilistic amplification model

Convolve reference hazard with amplification model:

$$\lambda_{IM^z}(im_z) = \int_0^\infty P(IM_z > im_z | IM_x = im_x) |d\lambda_{IM^x}(im_x)|$$



# Convolution

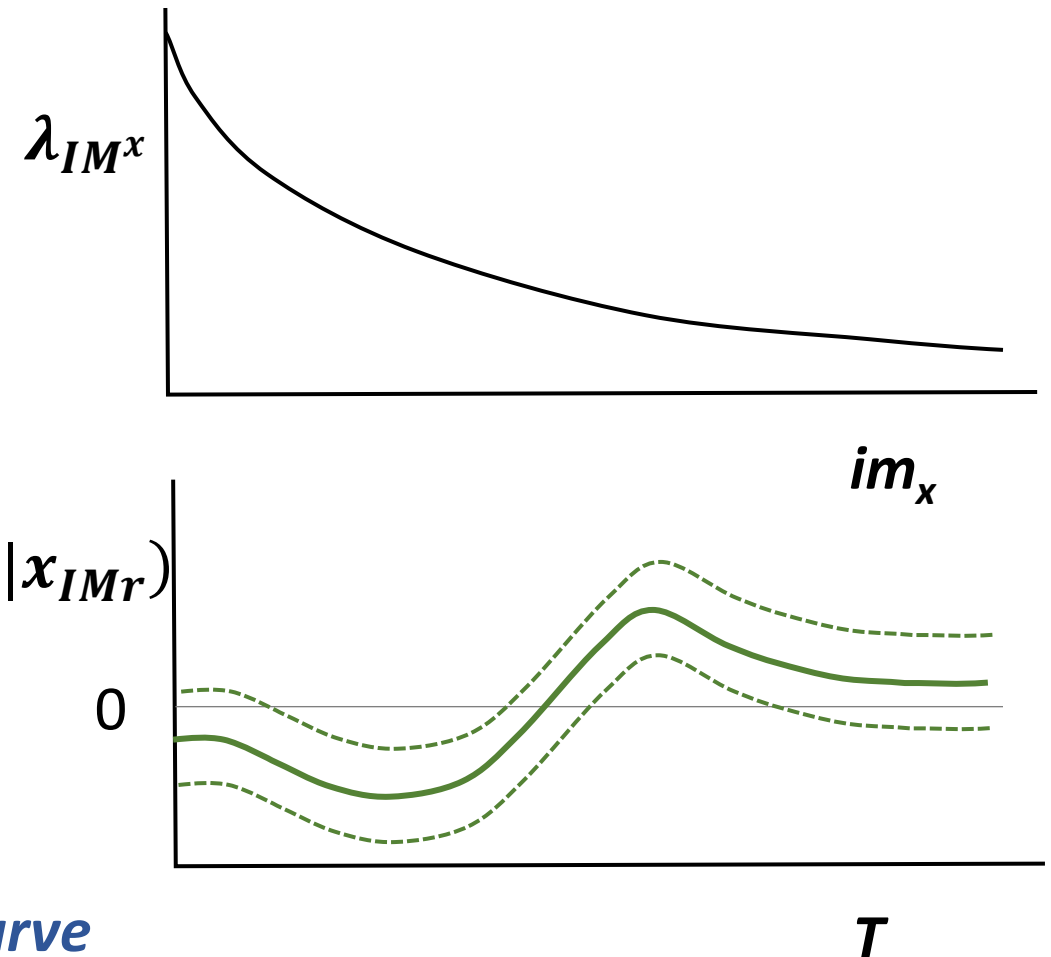
Develop reference site ( $X$ ) hazard curves & UHS ordinates

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Convolve reference hazard with amplification model:

$$\lambda_{IM^z}(im_z) = \int_0^\infty P(IM_z > im_z | IM_x = im_x) |d\lambda_{IM^x}(im_x)|$$

*Slope of hazard curve*



# Convolution

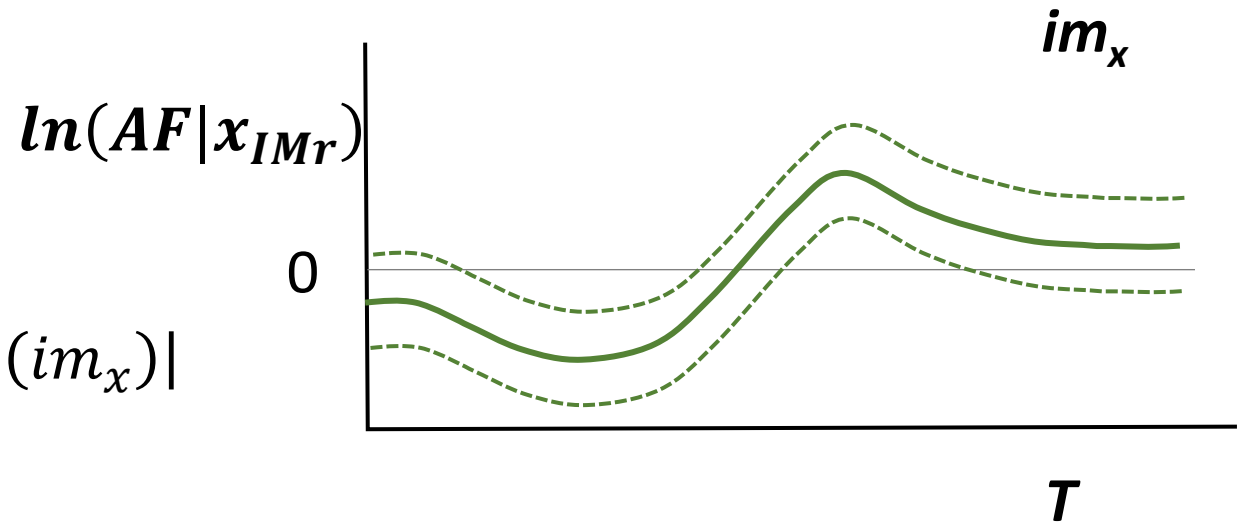
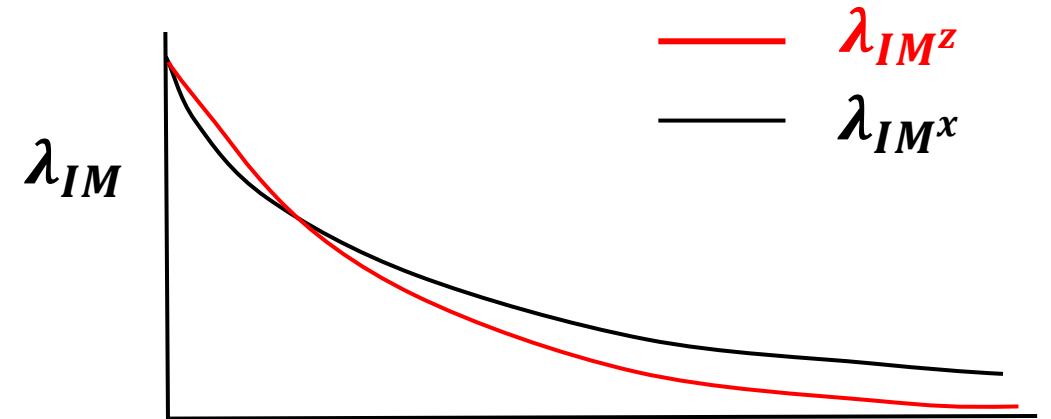
Develop reference site (X) hazard curves & UHS ordinates

Develop  $x_{IMr}$ -dependent probabilistic amplification model

Convolve reference hazard with amplification model:

$$\lambda_{IM^z}(im_z) = \int_0^{\infty} P(IM_z > im_z | IM_x = im_x) |d\lambda_{IM^x}(im_x)|$$

**Probability computed using amplification function**



# Convolution

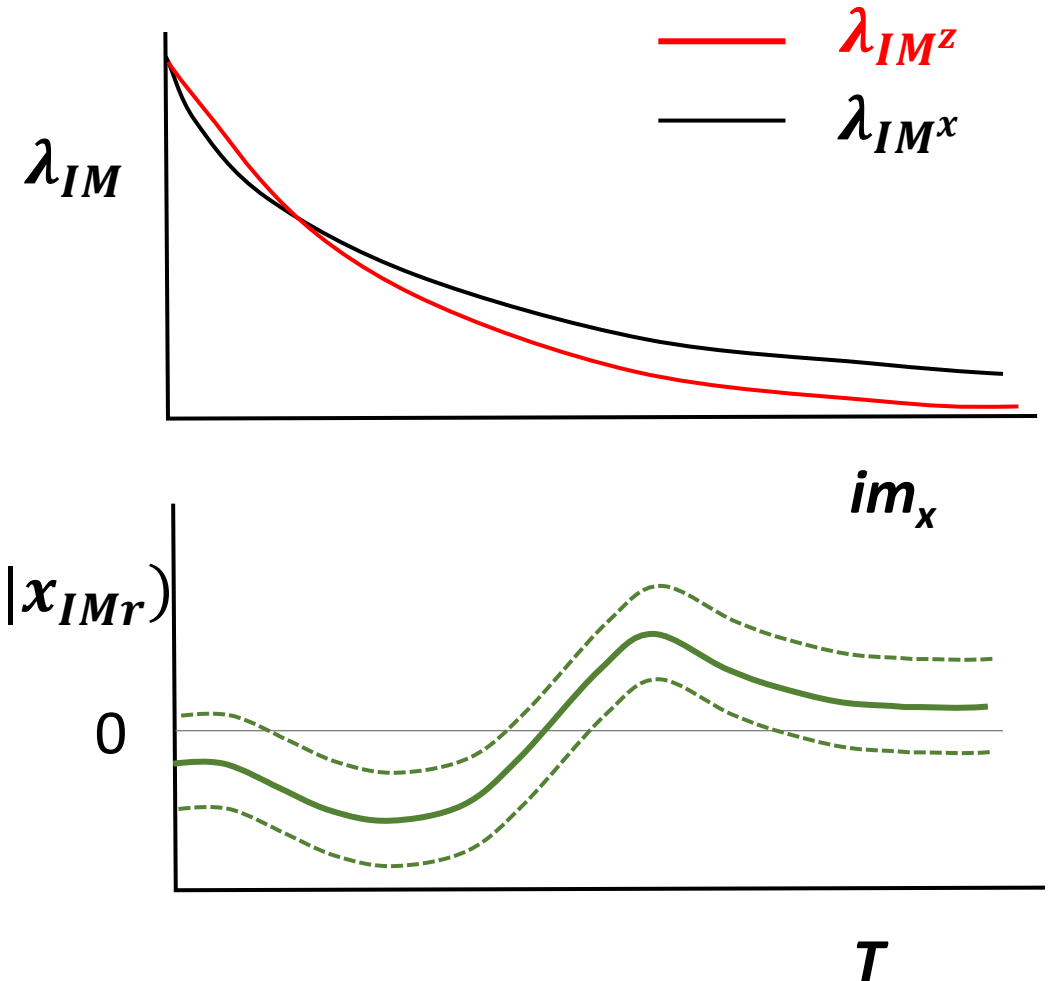
Develop reference site ( $X$ ) hazard curves & UHS ordinates

Develop  $x_{IMr}$ -dependent probabilistic amplification model

Convolve reference hazard with amplification model:

$$\lambda_{IM^z}(im_z) = \int_0^\infty P(IM_z > im_z | IM_x = im_x) |d\lambda_{IM^x}(im_x)|$$

NRC Approach 3 (Bazzurro and Cornell, 2004)



# Modified GMM

Select GMMs

Remove ergodic site terms

Add site-specific mean site term, being sure to maintain reference condition

Modify aleatory variability & implement logic tree that accounts for site response uncertainty

Run PSHA with modified GMM

NRC Approach 4

# Site-specific approach

Functional definitions

Model elements

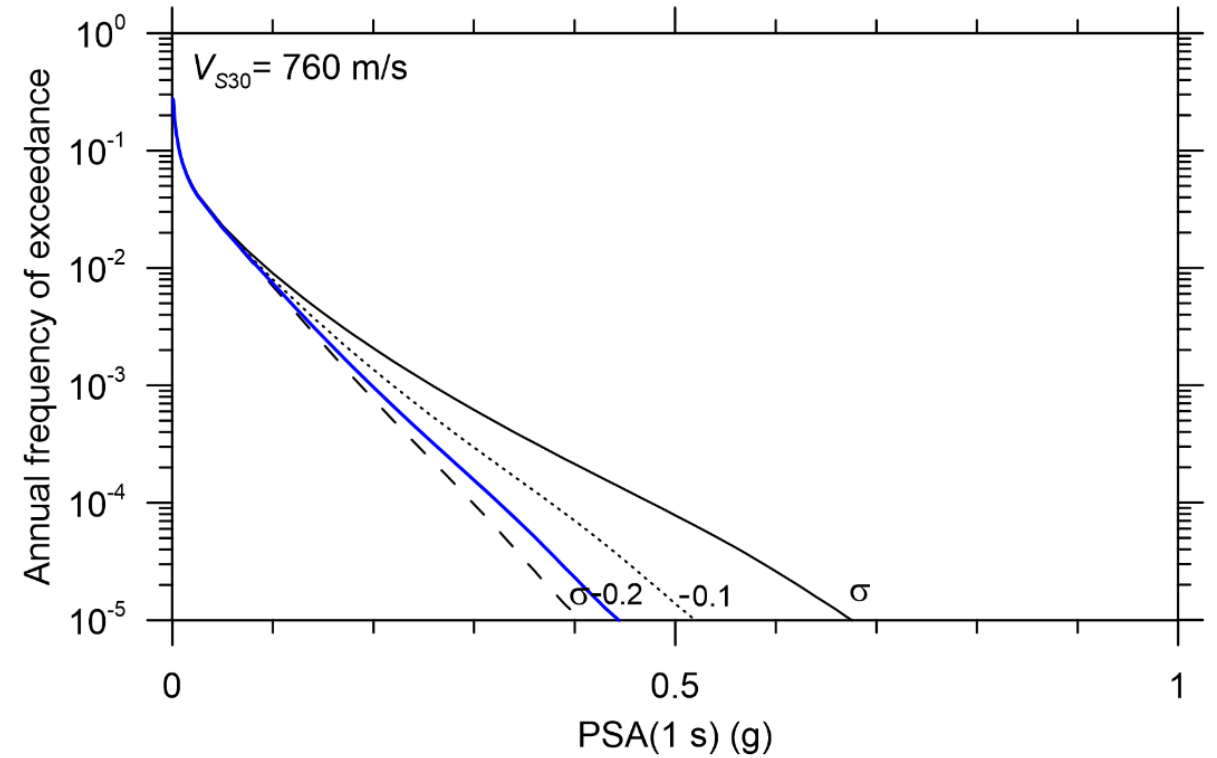
Implementation in hazard  
calculations

## **Example results**

Allowable reductions

# Example results

Steepens hazard curve slopes



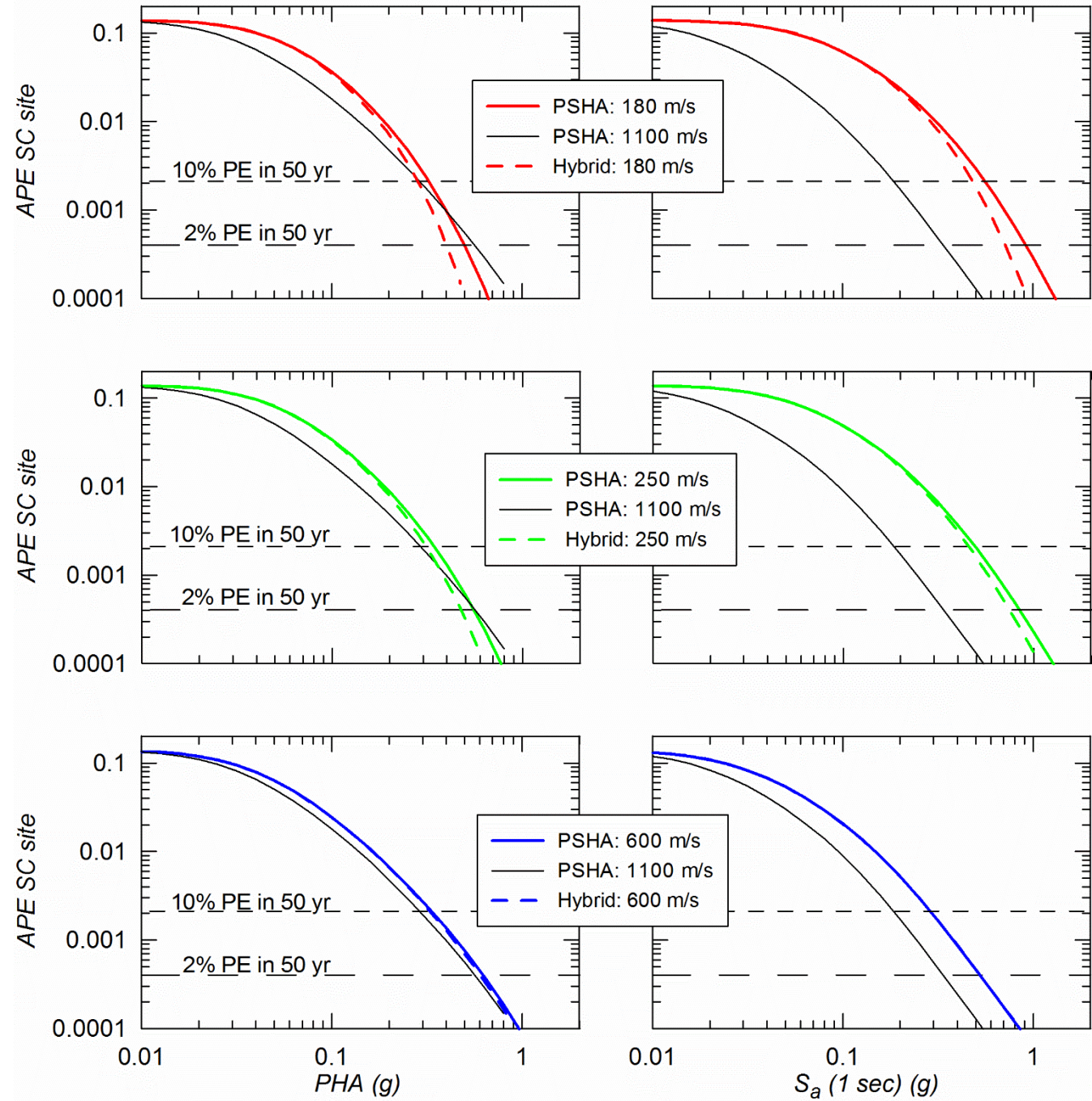
# Example results

Steepens hazard curve slopes

Hybrid vs. hazard integral implementation

Comparison of hazard curves derived from PSHA and the hybrid procedure at Los Angeles site location for three site conditions. Goulet et al. (2009)

Los Angeles, California Site

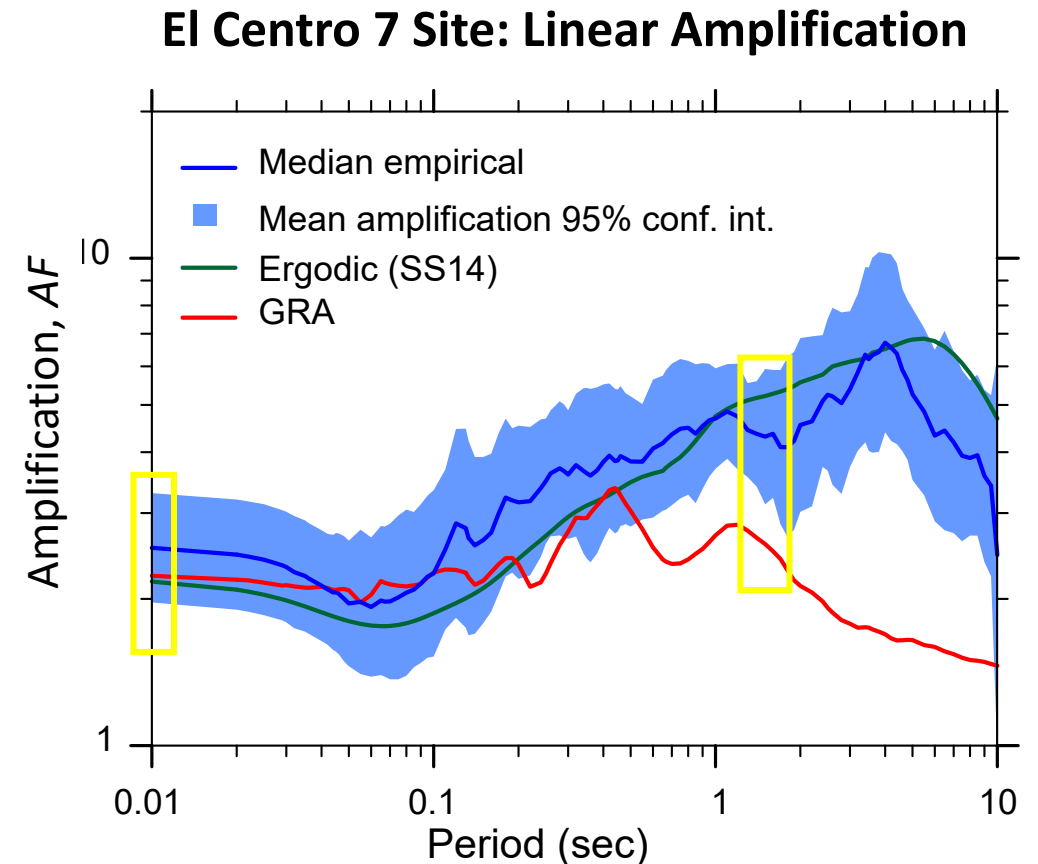


# Example results

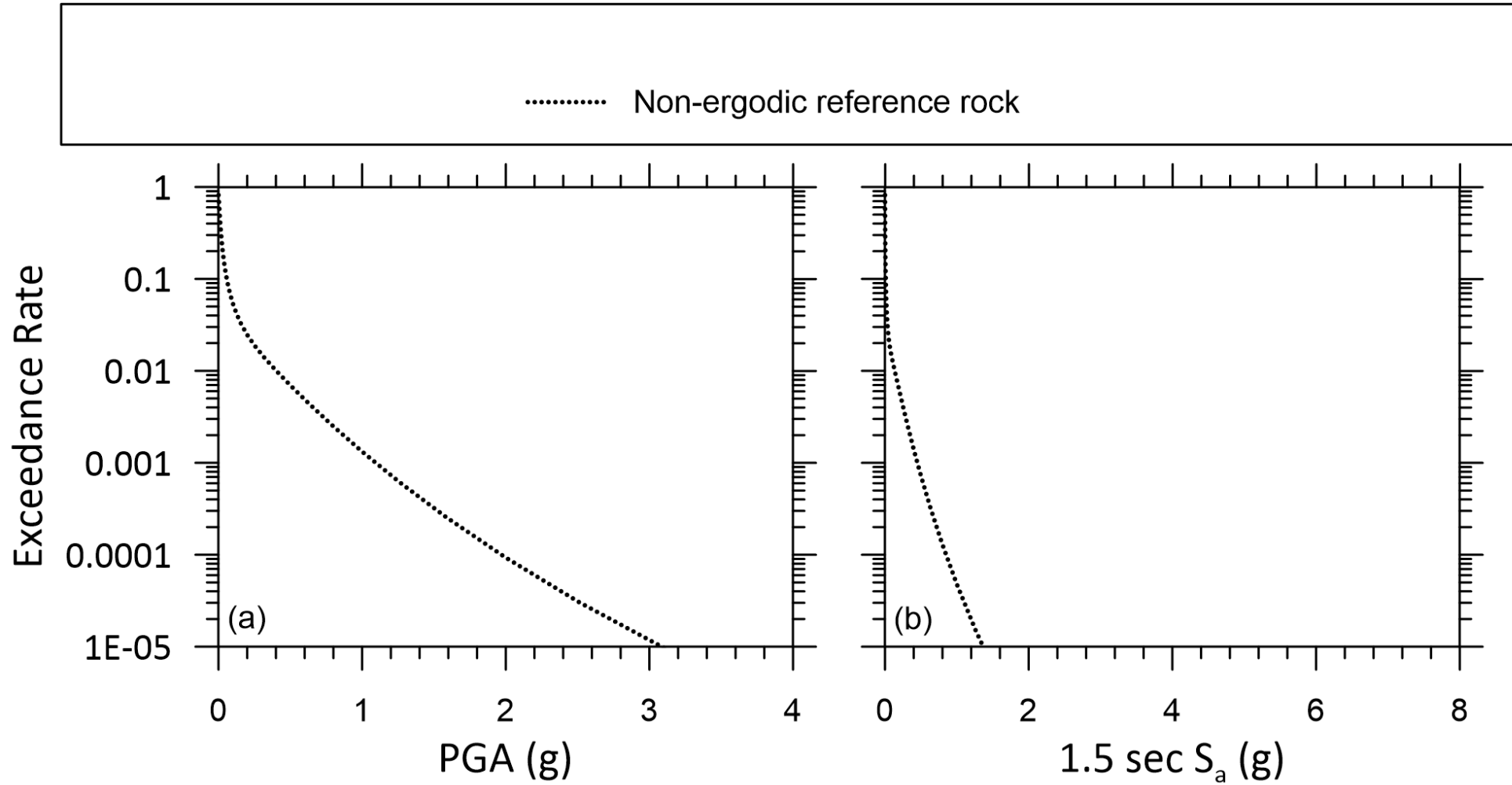
Steepens hazard curve slopes

Hybrid vs. hazard integral  
implementation

Convolution implementation vs.  
ergodic

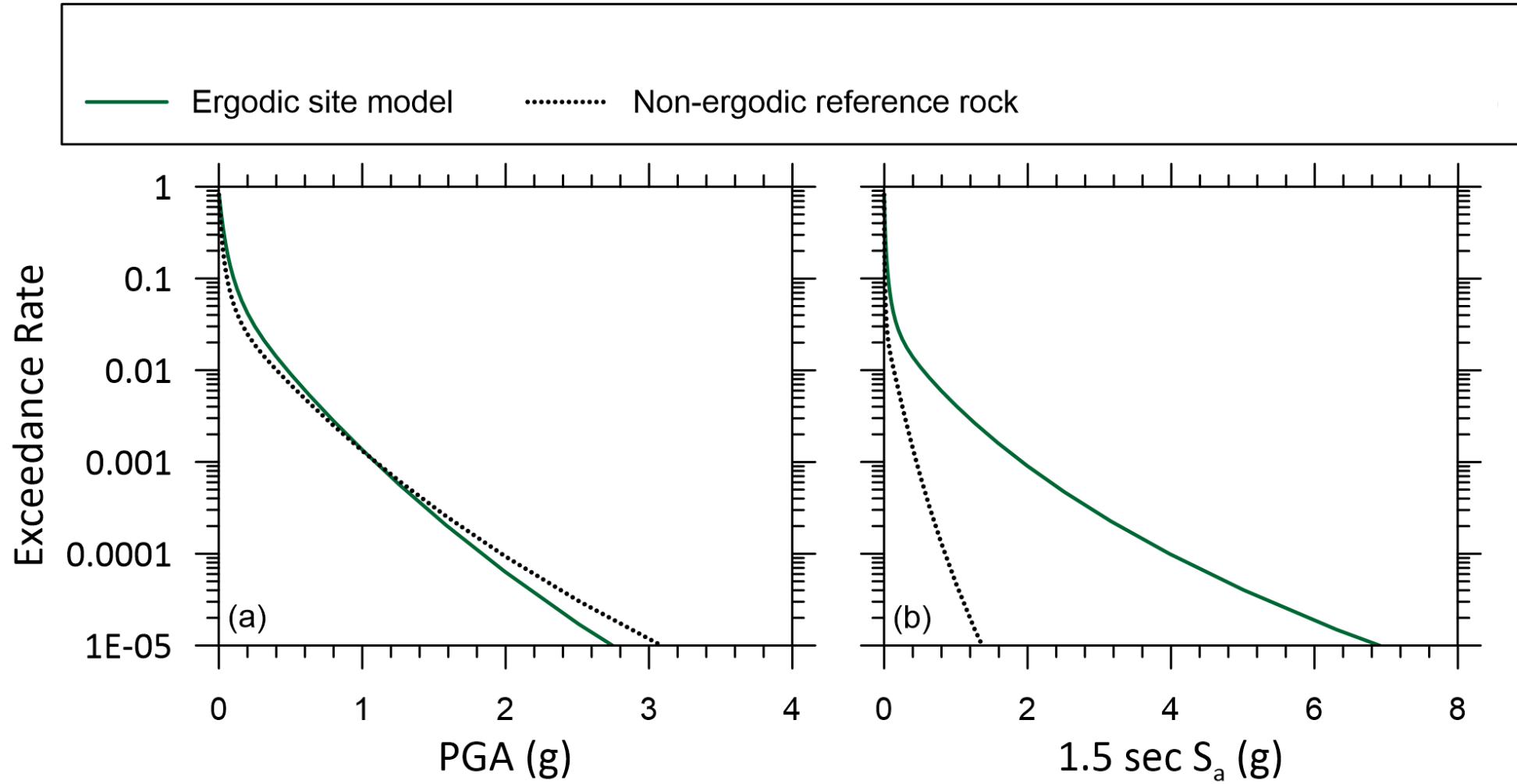


# El Centro 7 site (soft soil)



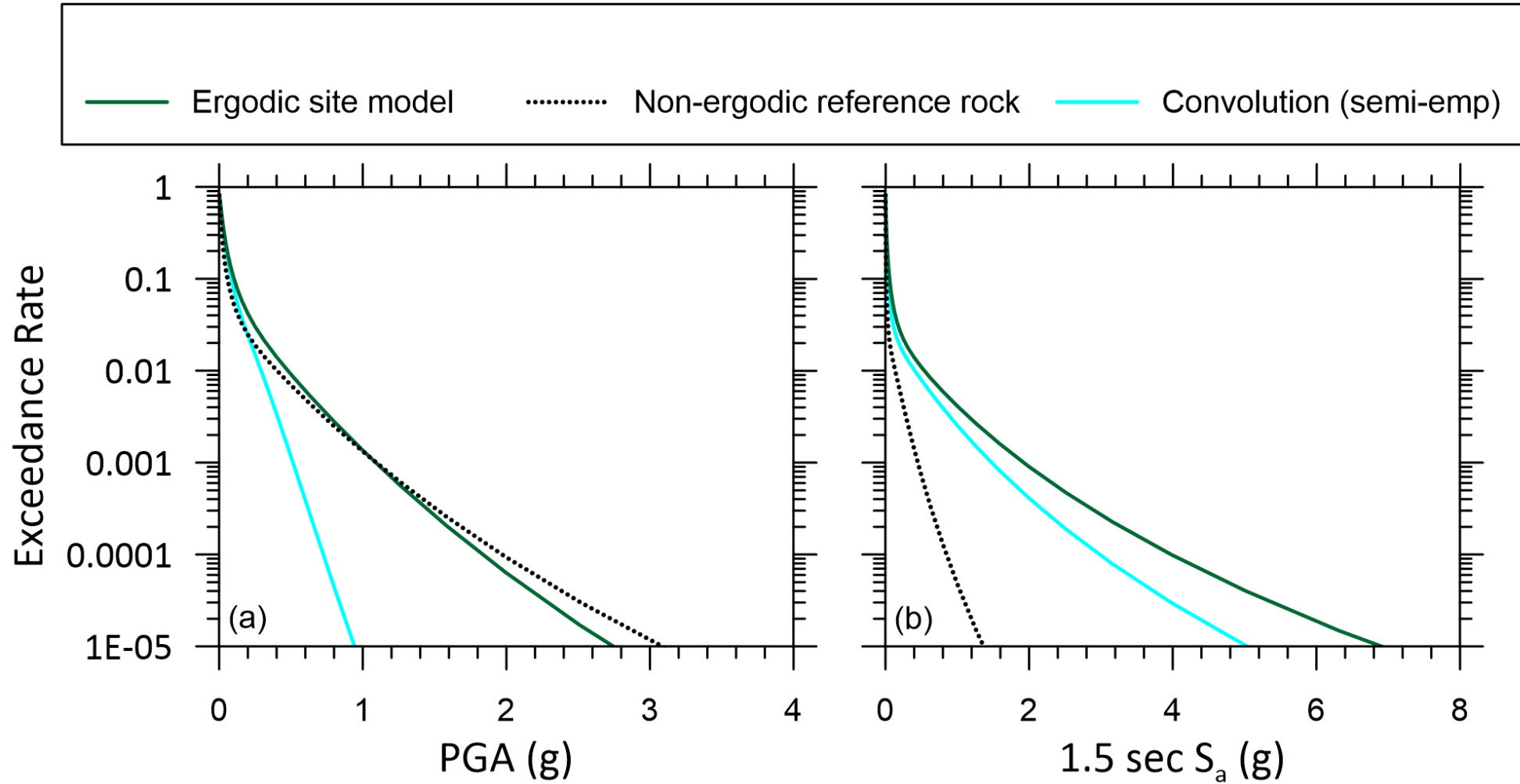
*Modified from Stewart et al. 2017*

# El Centro 7 site (soft soil)



*Modified from Stewart et al. 2017*

# El Centro 7 site (soft soil)



*Modified from Stewart et al. 2017*

# Site-specific approach

Functional definitions

Model elements

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Example results

**Allowable reductions**

## *Allowable reductions*

Point of comparison is  $MCE_R$  spectrum from USGS seismic design Geo-Database

NEHRP 2020 (ASCE-7/22) and before: maximum 20% reduction

NEHRP 2026, site-specific approach: maximum 30% reduction

# Outline

Current procedures

Issues motivating new procedures

Site-specific site response approach

**Hybrid ground motions approach**

Other technical improvements

Organization and status of document

# Hybrid ground motions approach

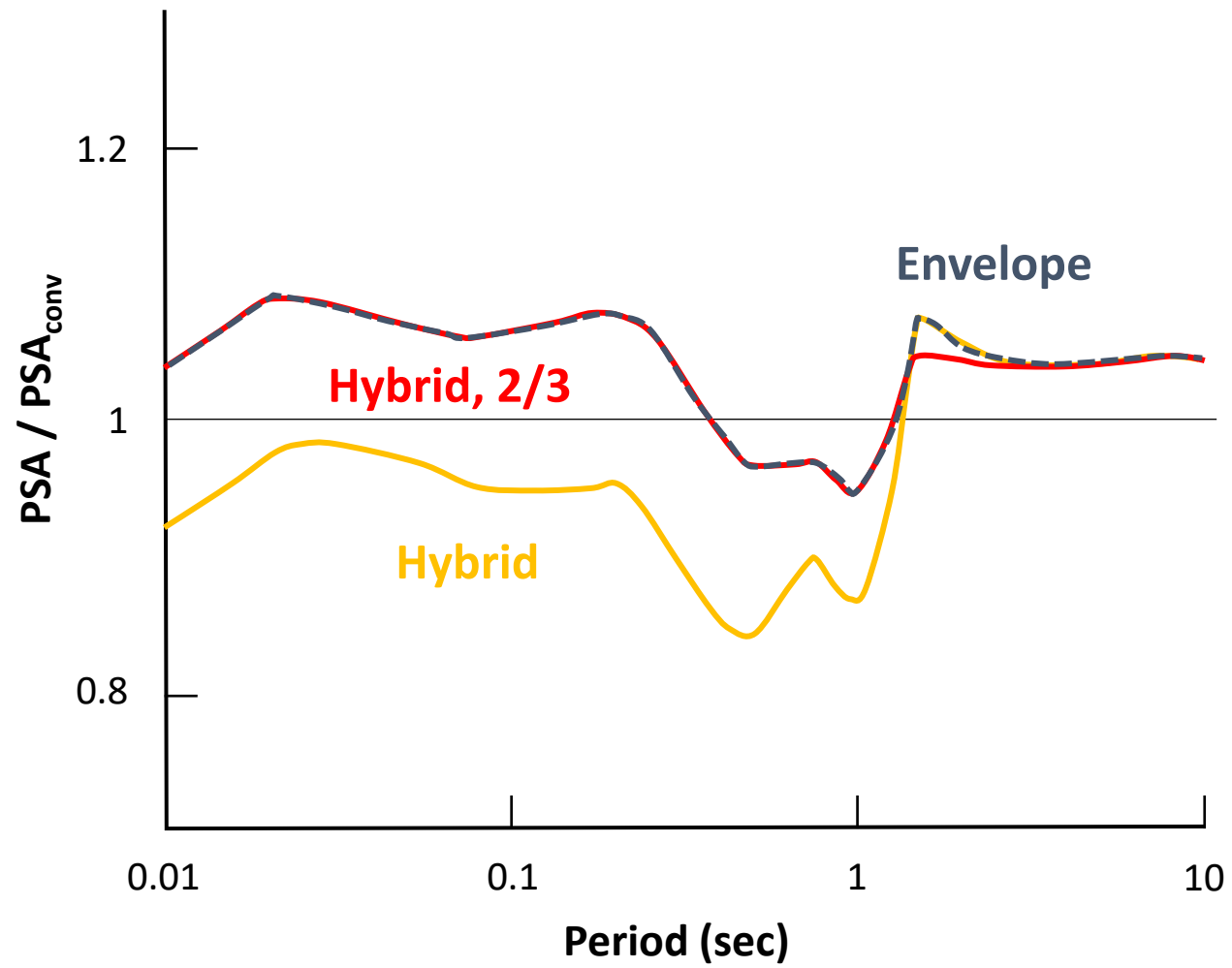
Amplification computed using GRA with  $MCE_R$  and  $\frac{2}{3}MCE_R$

No amplification models ( $f_1, f_2, f_3$ ) required

Hazard computed using full  $\phi_{S2S}$  ( $IM^{ref}$ )

Enveloped hybrid approach,  $IM^{surf} = \max(AF^{MCE_R}, AF^{\frac{2}{3}MCE_R}) \times IM^{ref}$

Max 20% reduction



# Outline

Current procedures

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Site-specific site response approach

Hybrid ground motions approach

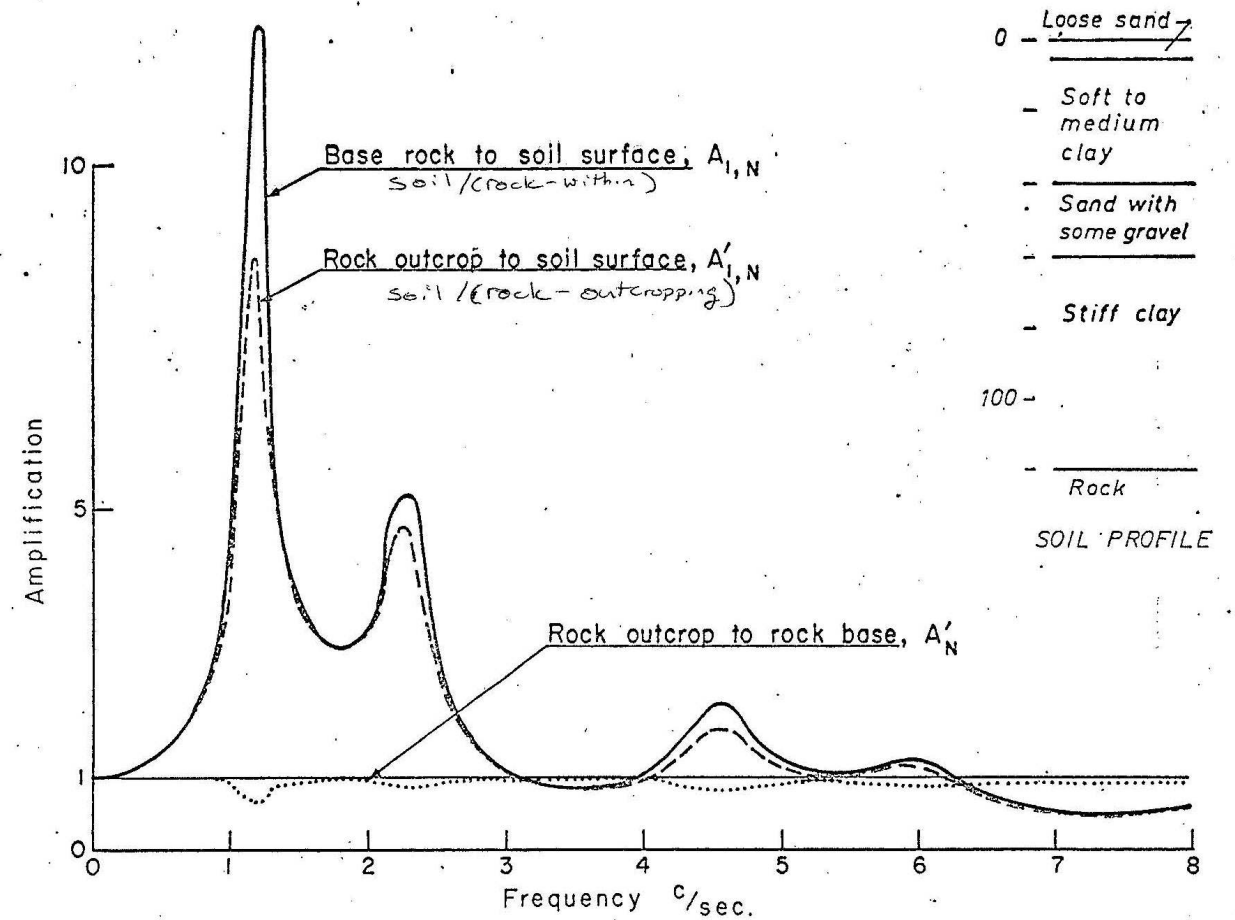
**Other technical improvements**

Organization and status of document

# Other technical improvements

## Long period problem

- GRA usable for  $T \leq xT_{site}$  ( $x \sim 1-2$ )

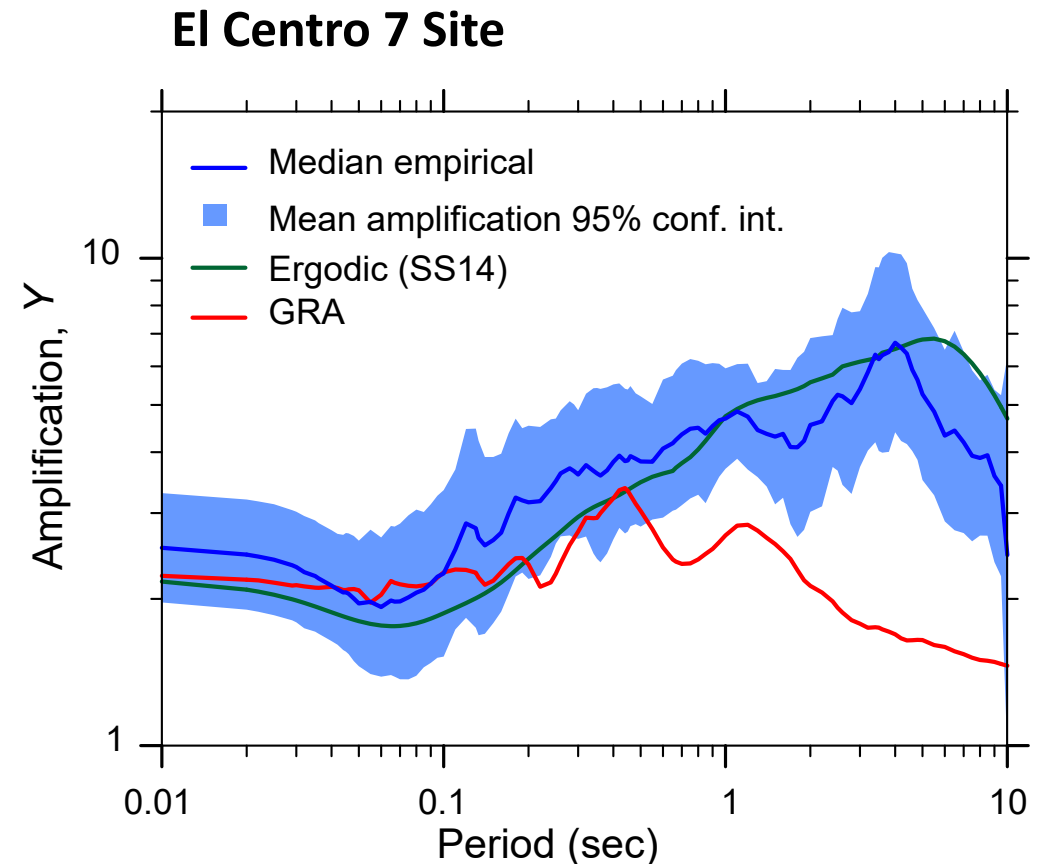


Transfer functions for elastic site response. Schnabel, 1973

# Other technical improvements

## Long period problem

- GRA usable for  $T \leq xT_{site}$  ( $x \sim 1-2$ )
- Example results
- Fix by transitioning to ergodic model for  $T > xT_{site}$



# Other technical improvements

Long period problem

## Site characterization

- $V_S$  profiles – credible methods

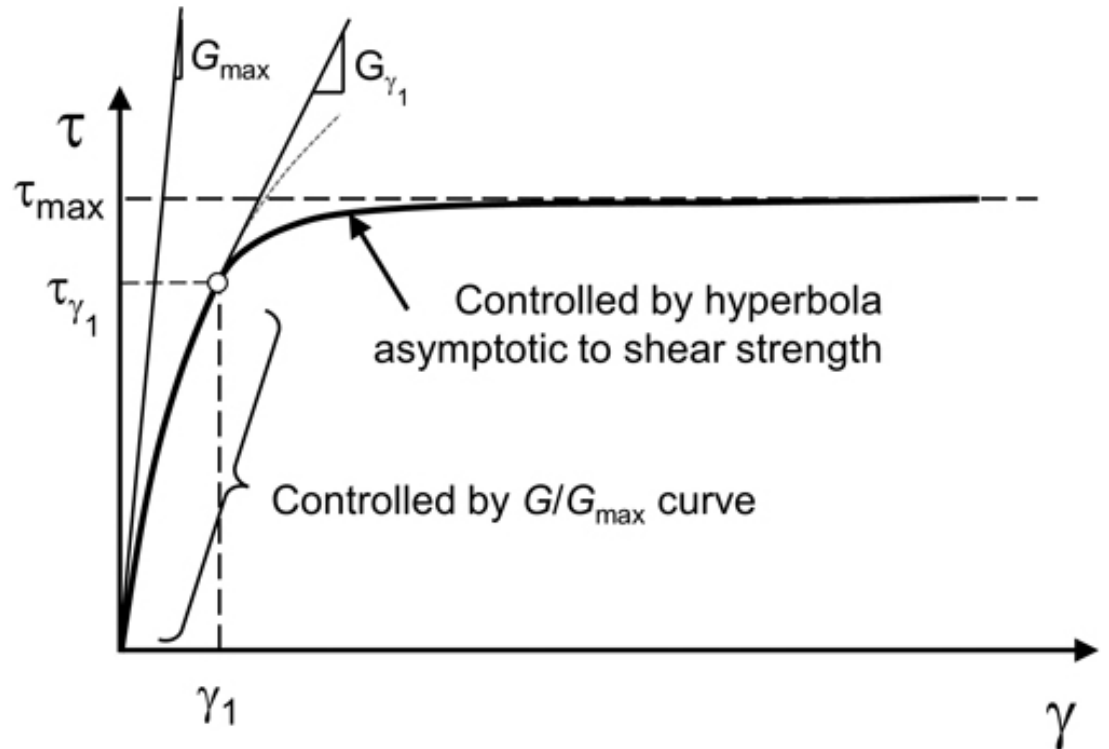
“Methods based on a single-direction linear array of surface instruments without a controlled vibration source are considered not credible in this standard and shall not be used for the derivation of  $V_S$  profiles.”

# Other technical improvements

Long period problem

## Site characterization

- $V_s$  profiles – credible methods
- Adjust modulus reduction curves for shear strength if large strains develop



*Kramer & Stewart 2025*

# Other technical improvements

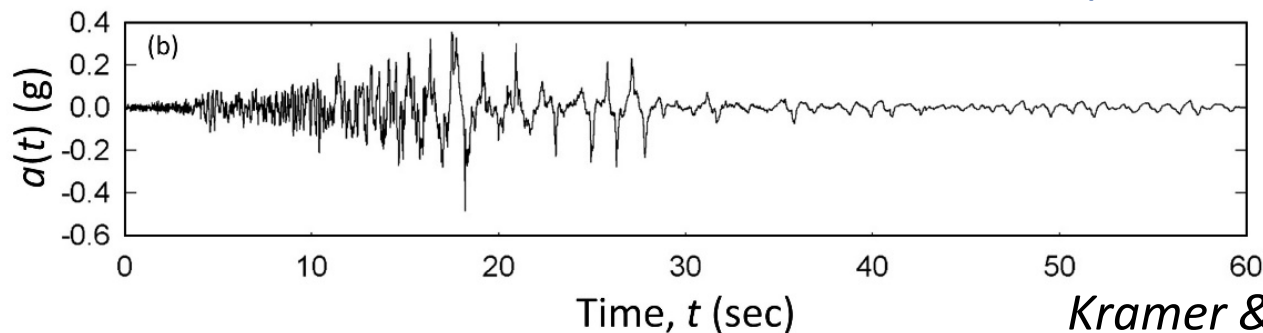
Long period problem

Site characterization

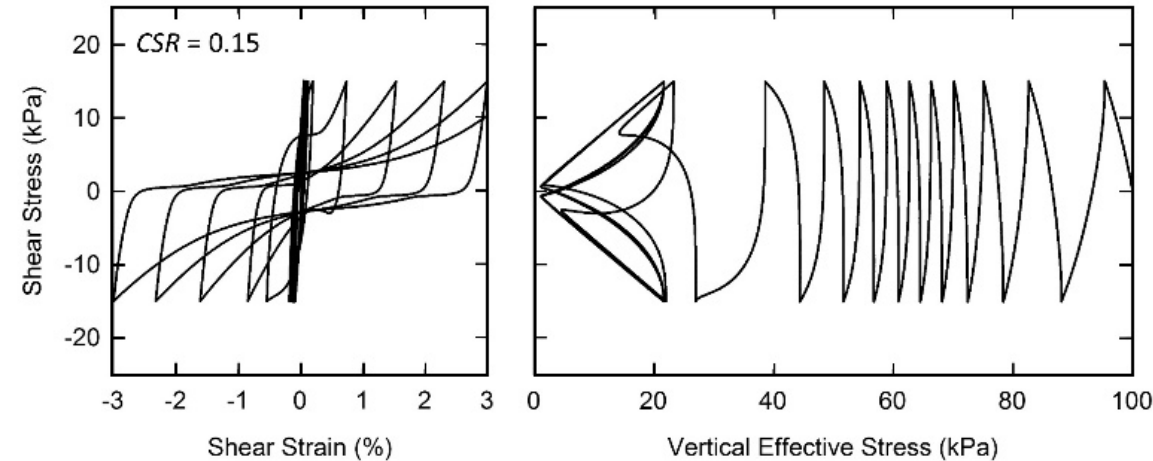
## Modeling liquefaction

- Constitutive models that capture phase transformation (generally) required

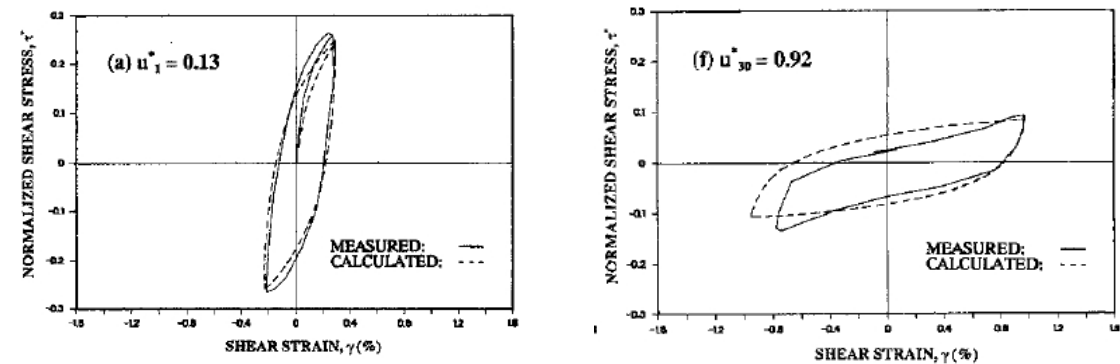
Kushiro Port record from Kushiro-Oki earthquake



## Model with dilation



## Model without dilation



# Outline

Current procedures

Issues motivating new procedures

Site-specific site response approach

Hybrid ground motions approach

Other technical improvements

**Organization and status of document**

# Organization

## Introduction

21.1.1: Reference site motion

21.1.2: Site properties model

21.1.3: Site response modeling

21.1.4: Ground motion variability and uncertainty

21.1.5: Analysis of ground motion hazard including site response

# Organization

## Introduction

- Charging language
- Definitions of *Site-specific site response* and *Hybrid ground motions*
- *Site-specific site response* requires peer review

# Organization

## 21.1.1: Reference site motion

- *Site-specific site response* requires either hazard curves or UHS for reference site. Various ways to define reference site provided
- *Hybrid* requires reference site  $MCE_R$
- Depending on GRA methods, need time series or spectra

# Organization

## 21.1.2: Site properties model

- $V_s$  profiles, MRD
- Liquefaction modeling guidelines, including consideration of phase transformation behavior
- Consider uncertainties

# Organization

## 21.1.3: Site response modeling

- *Site-specific site response*: define mean amplification function and uncertainty (Approach 1 or 2). Procedures to address long-period problem.
- *Hybrid*: no amp function, amp factors derived using  $MCE_R$  input and scaled version thereof (2/3). Addresses long period problem.

# Organization

## 21.1.4: Ground motion variability and uncertainty

- *Site-specific site response*: can eliminate  $\phi_{S2S}$ .
- *Hybrid*: cannot eliminate  $\phi_{S2S}$ .

# Organization

## 21.1.5: Analysis of ground motion hazard including site response

- *Site-specific site response*: convolution or modified GMM in hazard integral
- *Hybrid*: enveloping procedure for site amp. Envelop used to adjust  $MCE_R$  (reference site) to  $MCE_R$  (ground surface)

# Status

Approved for 2026 *NEHRP Provisions and Commentary*

ASCE 7-28:

- Approved by TC1 and SSC
- Resolution of comments from main committee pending

# Closure

New site-specific procedure introduced to the *Provisions*

A hybrid approach is retained, allowing continuation of current practice, but with tweaks to avoid unconservatism

We advanced this proposal because:

- Non-ergodic site response is being used; needs to be reflected in *NEHRP Provisions & Commentary* for guidance / guardrails
- Current procedures in Sec. 21.1 frequently unconservative
- Other improvements were needed

## References

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